

**Direction des Études et Synthèses Économiques**

**G 2013 / 05**

**Interpretation and limits of sustainability tests  
in public finance**

**Gildas LAMÉ, Matthieu LEQUIEN  
and Pierre-Alain PIONNIER**

**Document de travail**



**Institut National de la Statistique et des Études Économiques**

# INSTITUT NATIONAL DE LA STATISTIQUE ET DES ÉTUDES ÉCONOMIQUES

*Série des documents de travail  
de la Direction des Études et Synthèses Économiques*

**G 2013 / 05**

## **Interpretation and limits of sustainability tests in public finance**

**Gildas LAMÉ\*, Matthieu LEQUIEN\*  
and Pierre-Alain PIONNIER\***

MARCH 2013

The authors thank Guillaume Cléaud, Virginie Coudert, Élise Coudin, Éric Dubois, Corinne Prost, Lukas Reiss and participants at the Banque de France / BETA Conference on Macroeconomic and Financial Vulnerability Indicators in Advanced Economies (Strasbourg, September 2012) for comments on earlier versions.

---

\* Département des Études Économiques - Division Études Macroéconomiques, CREST  
Timbre G220 - 15, bd Gabriel Péri - BP 100 - 92244 MALAKOFF CEDEX

# Interpretation and limits of sustainability tests in public finance

## Abstract

Public debt is considered sustainable if discounted net repayments are expected to cover the initial debt issuance, i.e. if the government intertemporal budget constraint is expected to hold. With risk averse lenders and an uncertain economic environment, Bohn (1995) stresses that this constraint relies on a stochastic discount factor which depends on lenders' preferences. To get round the difficulty related to the specification of private agents' preferences in empirical analysis, Bohn (1998) suggests to estimate fiscal reaction functions describing how primary surplus reacts to indebtedness. After having solved the econometric issues arising when primary surplus and debt have a very different persistence (with a non-parametric approach) or are both integrated (with parametric tests), we estimate fiscal reaction functions for France and for Greece. The empirical results highlight the remaining limitations and interpretation difficulties that plague these econometric sustainability tests.

**Keywords:** Intertemporal budget constraint; unit-roots; cointegration; fiscal reaction function; non-parametric tests

---

## Interprétation et limites des tests de soutenabilité des finances publiques

## Résumé

La dette publique est dite soutenable lorsque la somme actualisée des remboursements anticipés couvre l'émission initiale de dette, c'est-à-dire lorsque la contrainte budgétaire intertemporelle de l'État est vérifiée. Dans un contexte où les prêteurs sont averses au risque et où l'environnement économique est incertain, Bohn (1995) montre que cette contrainte fait intervenir un facteur d'escompte stochastique qui dépend des préférences des agents. Afin de contourner la difficulté liée à la spécification de ces préférences dans les études empiriques, Bohn (1998) suggère d'estimer des fonctions de réaction fiscale décrivant comment le surplus primaire réagit à l'endettement. Après avoir résolu les difficultés qui se présentent en pratique lorsque le surplus primaire et la dette ont des persistances très différentes (avec une approche non-paramétrique) ou sont tous les deux intégrés (avec une approche paramétrique), nous estimons des fonctions de réaction fiscale pour la France et pour la Grèce. Les résultats mettent en évidence le fait que les tests économétriques de soutenabilité présentent des difficultés d'interprétation et des limites importantes, même lorsqu'ils sont correctement spécifiés.

**Mots clés :** Contrainte de budget intertemporelle ; racine unitaire ; cointégration ; fonction de réaction fiscale ; tests non-paramétriques

**Code JEL :** C12, E62, F34, H60, H62

# Contents

<b>Introduction</b>	<b>4</b>
<b>I Literature review on usual indicators and tests</b>	<b>5</b>
I.1 Frequently used indicators . . . . .	5
I.2 Economic framework . . . . .	6
I.3 Usual econometric tests and their limits . . . . .	7
<b>II Transversality condition and stochastic discount factor</b>	<b>9</b>
II.1 Transversality condition with stochastic discount factor . . . . .	9
II.2 About the example presented by Bohn (1995) . . . . .	11
<b>III Empirical results</b>	<b>12</b>
III.1 Data description . . . . .	13
III.2 Estimation of a fiscal reaction function when primary surplus and debt are integrated . . . . .	15
III.3 Estimation of a fiscal reaction function when primary surplus and debt are both stationary, the latter being much more persistent than the former . . . . .	15
III.4 Non-parametric tests . . . . .	17
III.5 Empirical results for France . . . . .	18
III.6 Empirical results for Greece . . . . .	21
<b>Conclusion</b>	<b>25</b>
<b>A Appendix</b>	<b>26</b>
A.1 Sufficient sustainability condition based on the fiscal reaction function	26
A.2 Stationarity of the error term and the control variables is not sufficient	28
A.2.1 An example with weak stationarity . . . . .	28
A.2.2 An example with strong stationarity . . . . .	28
A.3 Debt cannot be at the same time $I(m)_{m \geq 0}$ in level and $I(k)_{k \geq 0}$ after discounting . . . . .	29
A.4 Proof of proposition I.1 . . . . .	29
A.5 Description of the French quarterly data . . . . .	30

## Introduction

Public debt sustainability is a major concern in Europe at least since the outbreak of the Euro Area sovereign debt crisis. Public debt dynamics in countries such as Greece is particularly monitored. But even before the Great Recession, many industrial countries showed persistent deficits and an increasing public debt. Evaluating the sustainability of fiscal policy had naturally come under the spotlight. The Pébereau (2005) and Champsaur-Cotis (2010) administrative reports illustrate this concern for France.

How to define a sustainable debt? A possible definition is given by the IMF (2002): debt has to “satisf[y] the present value budget constraint without a major correction in the balance of income and expenditure given the costs of financing [the government] faces in the market”. Obviously it is not straightforward to precisely determine what a “major correction” is. Does it refer to a change in the reaction function of government’s revenue and spending to the business cycle or to public debt, or to a sizeable adjustment of public finances, without any change to the usual reaction function? If a government already has, in the past, taken successful measures to curb high indebtedness and faces again the same situation, should it be considered insolvent according to the IMF definition?

In this paper we favor the more usual term of sustainability over solvency. It refers to the ability of a government to pay back its debt with the discounted sum of the primary surpluses generated in the future. As Wyplosz (2007) noticed, the notion of sustainability is essentially forward-looking since it is the future balances that matter. Nevertheless public debt sustainability is often assessed with econometric tests on past data. Boissinot et al. (2004) concluded with standard tests that French public debt was (weakly) sustainable.

Potential behavioral breaks, in the past or between the end of the sample of available data and the near future, represent a first hurdle to interpret these tests’ results. From a logical point of view, the only question they give an answer to is: does the management of public finances as observed in the past justify that investors buy or refuse to buy public debt? Indeed rational investors buy debt securities only under the condition that the discounted repayments by the government cover the initial debt issuance, i.e. when they believe that the government intertemporal budget constraint holds.

Besides the possible behavioral breaks, Bohn (2007) has underscored that usual tests rely on sustainability conditions that are only sufficient. This weakens their interpretation. As long as investors keep on buying public debt securities, the rejection of a sufficient condition of sustainability can therefore be interpreted in two different ways. Either they expect the government to follow in the future a different policy because it can freely adjust its expenditures and receipts. Or they do base their analysis on the past behavior of public finances, but with different lenses than the econometrician, and another sufficient condition for sustainability could justify their buying of public debt.

Following a review of the usual tests and of the sufficient sustainability conditions they lean on, we focus on the specification of the government intertemporal budget constraint. Bohn (1995) has stressed that writing this constraint with the interest

rate on public debt is not always justified. With risk averse lenders and an uncertain economic environment, this constraint relies on a stochastic discount factor depending on lenders' preferences.

To get round the difficulty related to the specification of private agents' preferences in empirical analysis, Bohn (1998) suggests to estimate fiscal reaction functions describing how primary surplus reacts to indebtedness. We show that this procedure is valid only under strict technical assumptions and entails econometric difficulties. After having solved the econometric issues arising when primary surplus and debt have a very different persistence (with a non-parametric approach) or are both integrated (with parametric tests), we estimate fiscal reaction functions for France and for Greece in the last part of this study. The empirical results highlight the limitations and interpretation difficulties that plague these econometric sustainability tests. These difficulties are perfectly illustrated in the Greek case as the estimation of the fiscal reaction function on past data indicates that Greek public finances can be considered sustainable in 2007. Similar results for Greece are obtained by Mendoza and Ostry (2008) who also estimate fiscal reaction functions. Conversely, results of non-parametric and parametric tests in the French case are more mitigated but they do not indicate a significantly positive fiscal reaction function over the years 1978–2007. This result is at odds with subsequent developments. Indeed, French public debt has increased markedly after the end of the estimation sample, investors have continued to consider French public indebtedness as sustainable and borrowing costs have remained low, or even very low.

## I Literature review on usual indicators and tests

### I.1 Frequently used indicators

Public debt sustainability analysis generally starts from the debt accumulation equation:  $d_t = \frac{1+i_t}{1+y_t} d_{t-1} - s_t$ ,  $d_t$  being the end of period  $t$  stock of debt divided by GDP,  $i_t$  the interest rate,  $y_t$  the GDP growth rate and  $s_t$  the primary balance over GDP.

A simple and widely used indicator is the primary balance stabilizing the debt over GDP ratio. Primary balance (i.e.: balance before interest payments) is the variable under the short term control of the government. The stabilizing primary balance is given by the formula  $s_t^* = \left( \frac{1+i_t}{1+y_t} - 1 \right) d_t$ , or  $s_t^* \approx (\bar{i} - \bar{y}) d_t$ ,  $\bar{i}$  and  $\bar{y}$  being exogenous variables. The intuition is that a country able to stabilize its indebtedness without a major effort can be regarded as safe, a debt reduction requiring only a minimal further improvement of the primary balance. On the contrary, a debt stabilizing primary balance which cannot be reached without a substantial effort signals difficulties to control the evolution of public debt.

In the same spirit, the primary balance required to bring back debt to 60% of GDP (or whatever level considered to be safe) over a given period of time may be computed. Predictable costs to come can also be taken into account, typically the ageing costs (OECD; EC, 2011), or those stemming from a possible bailout of the banking system (Benassy-Quéré, 2012; EC, 2011).<sup>1</sup> The justification for such an

---

<sup>1</sup>This computation is harder to interpret because it involves episodes with very low probability but far-reaching consequences.

indicator is the following: if the effort to reach a given debt ratio within a reasonable horizon is deemed too large to be credible, then the country's sustainability can be questioned. The same ideas can be applied to government revenue (or spending) rather than to its surplus in order to answer the following question: by how much must taxes be raised to stabilize the debt to GDP ratio or to balance the budget (Blanchard, 1990)?

All these sustainability analysis are based upon the assumption of exogenous interest rates and GDP growth rates. They abstract from any feedback that fiscal policy may have on these variables (a deficit reduction is not neutral on the growth rate of the economy, either in the short or in the long run, nor on the interest rate). A solution to the first remark is to repeat the analysis with different scenarios for the path of the exogenous variables. If sustainability is accepted (respectively rejected) for a pessimistic (optimistic) scenario, one can be more confident in their diagnosis than with only a central scenario. However conflicting results, depending on the evolution scenarios for the exogenous variables, may also appear. This is the approach chosen by the IMF and the World Bank for their joint *Debt Sustainability Assessments*, which are studied by Wyplosz (2007). They consist in attaching probabilities to different scenarios for the years ahead and infer a range of possible levels for public debt.

## I.2 Economic framework

With  $D_t$  the end of period  $t$  stock of debt,  $r_t$  the interest rate and  $S_t$  the primary balance in period  $t$ , the accounting identity governing the evolution of the stock of debt is:  $D_t = D_{t-1}(1 + r_t) - S_t$ . Variables can be nominal, real or expressed as a ratio of GDP. The interest rate is thus respectively the nominal rate  $i_t$  paid on debt, the real rate or the rate defined by  $1 + r_t = (1 + i_t)/(1 + y_t)$ ,  $y_t$  standing for nominal GDP growth.  $D_t$  can be written as a function of expected surpluses with a simplifying assumption on future interest rates. The literature often considers  $r_t = r > 0$  constant, or  $\mathbb{E}_t[r_{t+1}] = r > 0$  for example. One obtains recursively:

$$D_t = \sum_{i=1}^N \frac{\mathbb{E}_t[S_{t+i}]}{(1+r)^i} + \frac{\mathbb{E}_t[D_{t+N}]}{(1+r)^N} \quad (1)$$

With rational lenders, the supply of debt meets a demand if the transversality condition (TC *ad hoc*) holds. It is the case when the expected debt discounted at a rate  $r$  converges to 0,<sup>2</sup> meaning that lenders expect that debt will be paid back in full through discounted expected primary surpluses, which is exactly the intertemporal budget constraint (IBC *ad hoc*):

$$D_t = \sum_{i=1}^{\infty} \frac{\mathbb{E}_t[S_{t+i}]}{(1+r)^i} \quad (\text{IBC } ad \text{ } hoc)$$

$$\lim_{N \rightarrow \infty} \frac{\mathbb{E}_t[D_{t+N}]}{(1+r)^N} = 0 \quad (\text{TC } ad \text{ } hoc)$$

Both preceding constraints are equivalent, and they are valid when debt is sustainable.

---

<sup>2</sup>This choice for the discount rate cannot be justified according to Bohn (1995), and it makes the transversality condition and the intertemporal budget constraint *ad hoc*. This issue will be addressed in section II.1.

Within this framework it appears that stabilizing the debt to GDP ratio is not a necessary sustainability condition. Debt can be regarded as sustainable even if the ratio of debt over GDP increases whenever the interest rate is larger than the growth rate, which is the case when the economy is dynamically efficient.

The relevant choice of the discount rate will be dealt with later (see II.1). For now we address the interpretation issue of the usual econometric tests: are they based on sufficient and necessary sustainability conditions, or only sufficient ones?

### I.3 Usual econometric tests and their limits

One of the first major contributions to the econometric literature on public debt sustainability is Hamilton and Flavin (1986).<sup>3</sup> In this article, the interest rate is constant: it is the *ex post* real interest rate earned on one-period government bonds over an average year. The authors test the transversality condition  $\lim_{N \rightarrow \infty} \frac{\mathbb{E}_t[D_{t+N}]}{(1+r)^{t+N}} = 0$  against the alternative that the limit exists and is strictly positive :  $\lim_{N \rightarrow \infty} \frac{\mathbb{E}_t[D_{t+N}]}{(1+r)^{t+N}} = A_0 > 0$ . Under the alternative and given past data, economic agents expect part of the debt never to be paid back. In this case the accounting identity (2) can be rewritten:

$$D_t = \mathbb{E}_t \sum_{i=1}^{\infty} \frac{S_{t+i}}{(1+r)^i} + A_0(1+r)^t \quad (2)$$

If debt follows a process of type (2) and if  $\{S_t\}$  is stationary, it is then equivalent to test the stationarity of  $D_t$  and the nullity of  $A_0$ . Hamilton and Flavin find that  $S_t$  and  $D_t$  are stationary<sup>4</sup> and infer the nullity of  $A_0$  and the sustainability of the American public debt.

Other authors have chosen an approach based on the variables determining debt's variation, such as the deficit or public spending and revenue.

Trehan and Walsh (1988) assume that the interest rate is constant and that revenue  $T_t$  and (without interest) spending  $G_t$  are at most  $I(1)$ . In this case, they show that the transversality condition (TC *ad hoc*) holds if total deficit (including interests) is stationary. This condition is equivalent to the existence of a cointegrating relationship between  $G_t^r$  (spending with interests) and  $T_t$  (revenue).

Quintos (1995) further proves that a  $I(2)$  debt is compatible with the transversality condition  $\lim_{N \rightarrow \infty} \frac{\mathbb{E}_t[D_{t+N}]}{(1+r)^N} = 0$ .<sup>5</sup> In this case, debt  $\mathbb{E}_t[D_{t+N}]$  behaves, in probability, like a polynomial in  $N$ ,<sup>6</sup> but this polynomial is asymptotically dominated by the exponentially-growing discount factor. Bohn (2007) broadens this result and proves

---

<sup>3</sup>These authors make substantial efforts to improve debt and deficit data (to subtract from the deficit the interest payments and the seigniorage revenue for instance, or to deal with the gold stock in the United States). The notation  $S_t$  is therefore slightly different in their paper.

<sup>4</sup>ADF test : rejection of the unit root hypothesis at 10 % (but not 5 %) for debt and primary balance.

<sup>5</sup>This is what Quintos (1995) calls weak sustainability. Boissinot et al. (2004) show that French public finances are weakly sustainable over the period 1978-2002 because general government's expenditures and receipts are bound by a cointegrating relationship  $T_t = \alpha + \beta \cdot G_t^r + \epsilon_t$  with  $0 < \beta < 1$ . However, they report that the coefficient  $\beta$  is declining over time and lower than in the U.S. and other European countries.

<sup>6</sup>One can use Bohn's (2007) proposition 1 to prove  $\mathbb{E}_t[D_{t+N}] = O_p(N^2)$  when  $D_t \sim I(2)$  process.

that sustainability holds when debt is integrated of arbitrarily high order (i.e.: when debt is  $I(m)$ ). Hence, the existence of a cointegrating relationship between revenue  $T_t$  and spending (including interests)  $G_t^r$  is not a necessary sustainability condition either. If these variables are integrated of orders  $m_T$  and  $m_G$  respectively, but not cointegrated, the order of integration of debt will be  $m$  with  $m \leq \max(m_1, m_2) + 1$ , ensuring that the transversality condition  $\lim_{N \rightarrow \infty} \frac{\mathbb{E}_t[D_{t+N}]}{(1+r)^N} = 0$  holds.

Procedures testing if debt is integrated of order  $m$ , against an alternative where its order of integration is strictly larger than  $m$ , therefore cannot reject the transversality condition. Sustainability holds both under the null and the alternative. In a nutshell, the null hypothesis is a sufficient but not necessary sustainability condition.

Trehan and Walsh (1991) do not restrict debt to be  $I(m)$ . They show that the transversality condition holds if primary surplus  $S_t$  and debt  $D_{t-1}$  are linked by a stationary linear combination ( $S_t - \alpha D_{t-1} = \epsilon_t \sim I(0)$ ) and if the quasi-difference of the primary surplus  $S_t - \lambda S_{t-1}$  with  $\lambda \in [0, 1+r[$  is  $I(0)$  and has a zero mean.<sup>7</sup> It follows:

$$D_t - \lambda D_{t-1} = (S_{t+1} - \lambda S_t) / \alpha - (\epsilon_{t+1} - \lambda \epsilon_t) / \alpha \sim I(0)$$

With  $\lambda$  in the interval  $]1, 1+r[$ , debt is explosive but sustainable because it is discounted by  $(1+r) > \lambda$ . Bohn (2007) notices that debt is not  $I(m)$  in this case, whatever the order of integration  $m$ . This underscores once again that having an  $I(m)$  public debt is just a sufficient sustainability condition, but not a necessary one.

Wilcox (1989) has a special place in the econometric literature on sustainability.<sup>8</sup> The variable of interest in his article is real debt discounted at date  $(t+i)$  with the realized yield on public debt between date  $t$  (reference year) and date  $(t+i)$ , i.e.:  $\frac{D_{t+i}}{(1+r)^i}$ . It is necessary for the transversality condition to hold that discounted real debt is stationary with its unconditional mean equal to zero.<sup>9</sup> In this case,  $\lim_{N \rightarrow \infty} \mathbb{E}_t[\frac{D_{t+N}}{(1+r)^N}] = 0$ . Estimating the unconditional mean of the discounted real debt is the purpose of Wilcox's test.

Wilcox's framework is not the same as in Bohn (2007) where it is debt in level (nominal or real) which is integrated of order  $m$ . It can be shown that debt cannot be at the same time  $I(m)$  in level and stationary after discounting (see annex A.3). It is however possible to generalize Bohn's results to a wider class of processes including those analyzed by Bohn and Wilcox (proof in annex A.4):

**Proposition I.1.** Let  $f$  be a deterministic and discrete function of time.

1. If  $D_{t+n}/f(n) \sim I(m)$ , with  $m \geq 0$  and  $f(n) = o((1+r)^n/n^m)$ , then debt verifies the transversality condition (TC *ad hoc*).

---

<sup>7</sup>Bohn (2007) notices that Trehan and Walsh (1991) implicitly consider a positive fiscal reaction function:  $S_t = \alpha D_{t-1} + \epsilon_t$  with  $0 < \alpha$ .

<sup>8</sup>However, it is not an isolated contribution. The method described by Wilcox (1989) has recently been adapted by Davig (2005) to allow for behavioral breaks in the data generating process of discounted debt.

<sup>9</sup>When discounted real debt is not stationary, two cases are possible: either the conditional mean  $\mathbb{E}_t[\frac{D_{t+N}}{(1+r)^N}]$  does not have a limit when  $n$  tends to infinity, or it is equal to a random variable and not necessarily to 0.

2. If  $D_{t+n}/f(n) \sim I(0)$  with  $f(n) = O((1+r)^n)$  and  $\mathbb{E}[D_{t+n}/f(n)] = 0$ , then debt verifies the transversality condition (TC *ad hoc*).

In particular, whatever  $r_0 < r$ ,  $D_{t+n}/(1+r_0)^n \sim I(m)$  is a sufficient condition for the ad hoc transversality condition to hold. Furthermore, if  $D_{t+n}/(1+r)^n \sim I(0)$  with mean zero, then the transversality condition also holds: it is the particular case studied by Wilcox (1989). Hamilton and Flavin (1986) also belong to this special case, since equation (2) shows that the conditions of the second case are verified when  $A_0 = 0$ . Finally the first case with a constant function  $f$  corresponds to the entire set of processes considered by Bohn (2007).

All the articles described so far make use of the interest rate on public debt in the transversality condition and, except Wilcox (1989), they make one of the following assumptions to characterize the evolution of this interest rate:

- $r_t = r > 0$ .
- $r_t$  is not autocorrelated and  $\mathbb{E}_t[r_{t+1}] = r > 0$ .
- $r_t$  is a stationary process with mean  $r > 0$ .

Beyond the interpretation issues related to the rejection of only sufficient conditions, the previous econometric tests show another weakness, associated with the choice of a very specific discount factor in the intertemporal budget constraint. We now come to this issue.

## II Transversality condition and stochastic discount factor

### II.1 Transversality condition with stochastic discount factor

In order to illustrate the choice of the relevant discount factor, we follow Bohn (1995) and consider a simplified endowment economy. At each date, a representative agent receives a random endowment  $Y_t$  that he cannot store. A fixed proportion  $g$  of this endowment is consumed by the government. This public consumption is financed by a tax and the issuance of government bonds to be repaid at a later date. In this decentralized economy, the Euler equation determines the government bond yield ensuring that households effectively consume a fraction  $(1 - g)$  of their endowment at each date. Using this Euler equation, one can price any security contingent on a specific state of nature being realized. We denote by  $s_t$  the different states of nature, by  $h_t = (s_t, h_{t-1})$  the history at date  $t$  and by  $\pi(s_t|h_{t-1})$  the probability of state  $s_t$  being realized conditional on history  $h_{t-1}$  at previous date.

Private agents maximize their intertemporal utility function:

$$\sum_{i=0}^{+\infty} \sum_{h_{t+i}} \beta^i \pi(h_{t+i}|h_t) U[C_{t+i}(h_{t+i})] = \mathbb{E}_t \left[ \sum_{i=0}^{+\infty} \beta^i U[C_{t+i}] \right]$$

Given the absence of arbitrage at the optimum, one can determine the price (i.e.: how many units of consumption goods) private agents are willing to invest at time  $t$  in exchange for one additional unit in the history  $h_{t+j}$  at time  $(t+j)$ :

$$q(h_{t+j}|h_t) = \beta^j \pi(h_{t+j}|h_t) \frac{U'[C_{t+j}(h_{t+j})]}{U'[C_t(h_t)]}$$

The yield of a government bond issued at time  $t$  and offering a total return  $(1 + r_t(j))^j$  in every state of nature at time  $t+j$  is given by the following formula:

$$\frac{1}{(1 + r_t(j))^j} = \sum_{h_{t+j}} \beta^j \pi(h_{t+j}|h_t) \frac{U'[C_{t+j}(h_{t+j})]}{U'[C_t(h_t)]} = \mathbb{E}_t \left[ \beta^j \frac{U'[C_{t+j}]}{U'[C_t]} \right]$$

In the same way, one can also price government debt at time  $t$  with payoff  $D_{t+n}(h_{t+n})$  at time  $t+n$  for every history  $h_{t+n}$ , given history  $h_t$ :

$$\sum_{h_{t+n}} \beta^n \pi(h_{t+n}|h_t) \frac{U'[C_{t+n}(h_{t+n})]}{U'[C_t(h_t)]} D_{t+n}(h_{t+n}) = \mathbb{E}_t \left[ \beta^n \frac{U'[C_{t+n}]}{U'[C_t]} D_{t+n} \right]$$

The relevant transversality condition in a stochastic environment becomes:

$$\lim_{n \rightarrow +\infty} \mathbb{E}_t \left[ \beta^n \frac{U'[C_{t+n}]}{U'[C_t]} D_{t+n} \right] = 0 \quad (\text{TC})$$

A strictly positive limit implies that private agents could have a higher intertemporal utility by consuming more at time  $t$  and lending less to the government. The country would then refinance itself indefinitely without ever fully repaying the principal as in a Ponzi scheme. Thus, rational investors would not be willing to hold such assets. By contradiction, this shows that the transversality condition (TC) always holds in equilibrium.

This condition is different from the usual transversality condition that is often used in the literature:

$$\begin{aligned} & \mathbb{E}_t \left[ \beta^n \frac{U'[C_{t+n}]}{U'[C_t]} D_{t+n} \right] \\ &= \mathbb{E}_t \left[ \beta^n \frac{U'[C_{t+n}]}{U'[C_t]} \right] \mathbb{E}_t [D_{t+n}] + \text{Cov}_t \left[ \beta^n \frac{U'[C_{t+n}]}{U'[C_t]}, D_{t+n} \right] \\ &= \frac{\mathbb{E}_t [D_{t+n}]}{(1 + r_t(n))^n} + \text{Cov}_t \left[ \beta^n \frac{U'[C_{t+n}]}{U'[C_t]}, D_{t+n} \right] \end{aligned}$$

Depending on the sign of the covariance term, it could be easier or more difficult for the usual transversality condition to hold. In the case of a deterministic economy or with risk-neutral private agents (with  $U[C_t] = \frac{C_t^{1-\epsilon}}{1-\epsilon}$ ,  $\epsilon = 0 \Rightarrow U'(C_{t+n}) = U'(C_t) = 1$ ), the transversality condition with uncertainty (TC) actually boils down to the usual (TC *ad hoc*). With risk-averse agents in a stochastic economy, both conditions will not in general coincide as it would require  $D_{t+n}$  and  $\beta^n \frac{U'[C_{t+n}]}{U'[C_t]}$  to be uncorrelated. Of course, it is unlikely to have a zero correlation between these two variables because (marginal utility of) consumption certainly depends on the

budgetary and fiscal stance of the government. Bohn (1995) provides an example in which the debt to GDP ratio remains constant. In this example, the *ad hoc* transversality condition can be rejected whereas the relevant one in a stochastic setting is always satisfied.

In a stochastic setting, the intertemporal budget constraint becomes:

$$D_t = \sum_{n \geq 0} \left\{ \frac{\mathbb{E}_t [T_{t+n} - G_{t+n}]}{(1 + r_t(n))^n} + \text{Cov}_t \left( \beta^n \frac{U'[C_{t+n}]}{U'[C_t]}, T_{t+n} - G_{t+n} \right) \right\} \quad (\text{IBC})$$

## II.2 About the example presented by Bohn (1995)

We consider the endowment economy defined previously and examine the case where the government issues debt so that the debt/GDP ratio measured at the end of each period and in every state of nature is constant:  $\frac{D_t(h_t)}{Y_t(h_t)} \equiv d$ . Taxes are adjusted so that public spending always represents a constant proportion  $g$  of the endowment  $Y_t$ . Equilibrium in the goods' market therefore implies that agents' consumption is a constant proportion of the endowment at each period:  $C_t = (1 - g)Y_t$ . This fiscal policy will be shown to be sustainable according to the transversality condition in a stochastic setting but not always with the usual one.

We use a CRRA instantaneous utility function with risk aversion denoted  $\epsilon^{10}$ :  $U[C_t] = \frac{C_t^{1-\epsilon}}{1-\epsilon}$ . The evolution of the endowment is supposed to be log-normal:  $\frac{Y_t}{Y_{t-1}} = 1 + y_t$  with  $\log(1 + y_t) \sim \mathcal{N}(\mu, \sigma^2)$ . Finally, we assume that the agents' intertemporal utility is finite given the properties of this process. Therefore the general term of this positive-term series converges to 0 as  $t$  approaches infinity.

$$\lim_{n \rightarrow +\infty} \mathbb{E}_t [\beta^n U[C_{t+n}]] = \frac{(1-g)^{1-\epsilon}}{1-\epsilon} \lim_{n \rightarrow +\infty} \mathbb{E}_t [\beta^n Y_{t+n}^{1-\epsilon}] = 0$$

Given our assumptions, the transversality condition in a stochastic setting holds. Indeed,

$$\lim_{n \rightarrow +\infty} \mathbb{E}_t \left[ \beta^n \frac{U'[C_{t+n}]}{U'[C_t]} D_{t+n} \right] = \frac{d(1-g)^{-\epsilon}}{U'[C_t]} \lim_{n \rightarrow +\infty} \mathbb{E}_t [\beta^n Y_{t+n}^{1-\epsilon}] = 0$$

We now write the risk-free rate on a loan between date  $t$  and date  $t + n$ :

$$\frac{1}{(1 + r_t(n))^n} = \mathbb{E}_t \left[ \beta^n \frac{U'[C_{t+n}]}{U'[C_t]} \right] = \mathbb{E}_t \left[ \beta^n \prod_{i=1}^n (1 + y_{t+i})^{-\epsilon} \right]$$

---

<sup>10</sup>A CRRA utility function is used in this example for the sake of simplicity. It is a well-known fact that this model does not allow to reproduce the pattern (i.e. the low values) of the risk-free interest rate with reasonable values of time preference, consumption volatility and risk aversion. But this example only aims at illustrating the differences between the stochastic discount factor and the riskless discount factor in a simple setting. Research in the joint modeling of economic fluctuations and asset returns is still active. We will circumvent the difficulty associated with the relevant specification of the stochastic discount factor in the empirical section of this paper.

We can then compare the riskless rate with the expectation of the debt variable at time  $t+n$  in order to see whether or not the usual transversality condition holds:<sup>11</sup>

$$\begin{aligned} \frac{1}{(1+r_t(n))^n} &= \beta^n \exp\left(-\epsilon\mu n + \frac{\epsilon^2\sigma^2 n}{2}\right) \\ \mathbb{E}_t[D_{t+n}] &= dY_t \mathbb{E}_t \left[ \prod_{i=1}^n (1+y_{t+i}) \right] = dY_t \exp\left(\mu n + \frac{\sigma^2 n}{2}\right) \\ \lim_{n \rightarrow +\infty} \frac{\mathbb{E}_t[D_{t+n}]}{(1+r_t(n))^n} &= 0 \Leftrightarrow (\epsilon-1)\mu - (1+\epsilon^2)\frac{\sigma^2}{2} - \log(\beta) > 0 \end{aligned}$$

For sufficiently high values of the risk aversion parameter  $\epsilon$  and of the variance  $\sigma^2$ , the usual transversality condition could be rejected whereas the relevant one in a stochastic setting would always be satisfied.

### III Empirical results

To get round the difficulty related to the estimation of a general equilibrium model and to the specification of private agents' preferences, Bohn (1998) suggests to estimate a fiscal reaction function describing how primary surplus reacts to public debt. He shows that a positive link is a sufficient condition for sustainability. The theoretical justification, given here in appendix, for estimating a fiscal reaction function is adapted from the unpublished appendix of Bohn (1998). We complement the original proof with an important precision concerning the control variables and the error term in the fiscal reaction function. The proof is relevant only if these variables are bounded. We provide a counter-example showing that it does not work with weakly stationary control variables and error term.<sup>12</sup> Details are available in the appendix at the end of the paper.

In practice, we will estimate the following regression where  $\mu_t$  comprises control variables and a structural error term:

$$\frac{S_t}{Y_{t-1}} = \alpha + \beta \frac{D_{t-1}}{Y_{t-1}} + \mu_t \quad (3)$$

It is slightly different from the one proposed by Bohn (1998), for two reasons. First, we change the date convention:  $D_t$  is now the end of period  $t$  debt whereas it is beginning of period  $t$  debt in Bohn (1998). Second, we divide primary surplus  $S_t$  and debt  $D_t$  by the GDP of period  $t-1$ . In this way, the right-hand-side variable  $\frac{D_{t-1}}{Y_{t-1}}$  is

---

<sup>11</sup>With the log-normal hypothesis made for the endowment variation, it can be inferred that :

$$\begin{aligned} \log(1+y_t) &\sim \mathcal{N}(\mu, \sigma^2) \\ \Rightarrow \log \prod_{i=1}^n (1+y_{t+i})^{-\epsilon} &\sim \mathcal{N}(-\epsilon\mu n, \epsilon^2\sigma^2 n) \\ \Rightarrow \mathbb{E}_t \left[ \prod_{i=1}^n (1+y_{t+i})^{-\epsilon} \right] &= \exp\left(-\epsilon\mu n + \frac{\epsilon^2\sigma^2 n}{2}\right) = (\mathbb{E}[(1+y_t)^{-\epsilon}])^n \end{aligned}$$

<sup>12</sup>In his 1998 paper, Bohn alternatively considers a stationary or a (strictly) bounded process  $\mu_t$ . In the appendix available on his web-page, he details the proof with a (strictly) bounded process only.

fully predetermined and the regression coefficient  $\beta$  is not subject to an asymptotic simultaneity bias. In the appendix, we prove that a significantly positive  $\beta$  in this specification ensures sustainability, relying on the additional assumption that the interest rate on public debt is bounded. In his specification, Bohn divides primary surplus and beginning of period  $t$  debt by the GDP of period  $t$ . He estimates the following regression, with his own date convention on debt:

$$\frac{S_t}{Y_t} = \alpha + \beta \frac{D_t}{Y_t} + \mu_t$$

Because GDP of period  $t$  depends on the primary surplus of period  $t$ , his estimation is subject to a simultaneity bias, even if  $D_t$  (beginning of period  $t$  debt) is predetermined.

This method entails other econometric difficulties when the persistence of the primary surplus is very different from the persistence of debt. We will describe a non-parametric method in order to deal with this econometric issue and apply it to French data. We will also consider Greek data where primary surplus and debt ratios are both integrated series. In this case, a parametric (cointegration) method will be considered. But first of all, we start with a description of the available data.

### III.1 Data description

French national accounts in base 2000 include a financial account for general government from 1978 on.<sup>13</sup> General government debt can be either defined as financial liabilities or as financial liabilities net of financial assets (gross debt or net debt thereafter). Notice that none of these definitions exactly match general government debt as it is defined in the Maastricht Treaty. In this treaty, debt consists in a subcomponent of general government's financial liabilities taken at their book value rather than at their market value.<sup>14</sup> It is also worth noting that debt, in the different definitions we consider, is never netted from non-financial assets such as land, buildings and infrastructures which are considered more difficult to liquidate if the government needs cash to repay creditors.

Moreover, Reinhart and Rogoff (2010) have constructed long time series of public debt for several countries including France. Reinhart and Rogoff's series for France coincides with general government debt as it is defined in the Maastricht Treaty after 1978. For the period before 1978, their series most likely represents financial liabilities of the central government only.

From an economic point of view, the most relevant variable seems to be (financial) net debt. Indeed, nationalizations and privatizations from the 1980s and 1990s led to movements of the same sign on the asset and liability sides of the general government balance sheet. Even if net debt may contain more measurement errors than gross debt, we will rely on it in the following for these economic reasons.

---

<sup>13</sup>Since May 2011, French national accounts are in base 2005 and encompass financial accounts since 1995 only. In the following, we rely on the last available accounts in base 2000.

<sup>14</sup>General government debt in the sense of the Maastricht Treaty is defined as the sum of total deposits (F2), securities excluding stocks and derivatives (F3 - F34) and credits registered on the liability side (F4) (cf. Bourges 2007). These aggregates are precisely defined in the 1993 System of National Accounts (1993 SNA).

Fiscal data available in the annual national accounts (base 2000) only cover a time span of 30 years (1978-2007). As quarterly national accounts in the same base are also available, it is possible to obtain a richer sample for our subsequent empirical analysis, i.e. net debt and primary surplus (structural or not) on a quarterly basis from 19801 to 2007Q4. Using net borrowing (B9A) as a quarterly indicator and Chow and Lin's (1971) method, we estimated a quarterly net debt for the general government. Moreover, we obtained a quarterly structural primary surplus, using a standard quadratic interpolation of annual potential GDP providing a quarterly output gap. Details on the construction of the quarterly data set are available in appendix A.5.

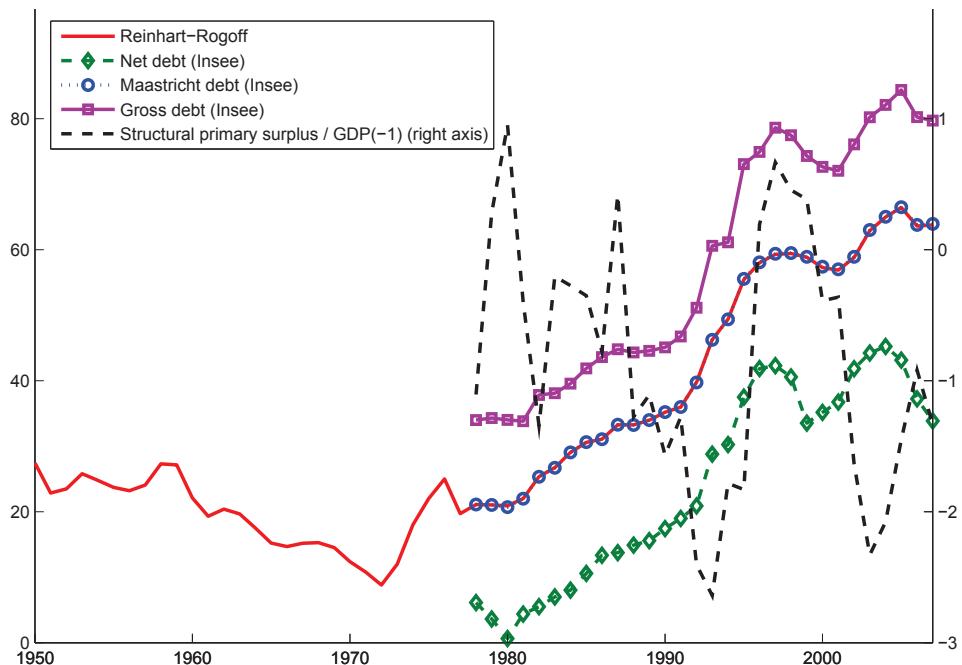


Figure 1: French public debt from 1949 to 2007 and structural primary surplus over 1978-2007 (% of GDP).

The evolution of Greek debt, primary and structural primary surpluses to GDP ratios is depicted on Figure 2. Greece has been able to reduce its primary deficit rapidly during the 1990s after its debt ratio had started to increase at the beginning of the 1980s. Afterwards, it maintained a positive primary surplus until 2002, allowing to stabilize the debt ratio around 100% of GDP. Only Maastricht debt is available for Greece in international databases. The structural primary surplus is obtained using the European Commission estimates of the output gap (AMECO database), and a budgetary sensitivity of 0.43 (as computed in European Commission, 2005). Unfortunately, the statistical approach used for France to obtain higher-frequency fiscal variables could not be replicated for Greece due to the lack of long enough quarterly national accounts.

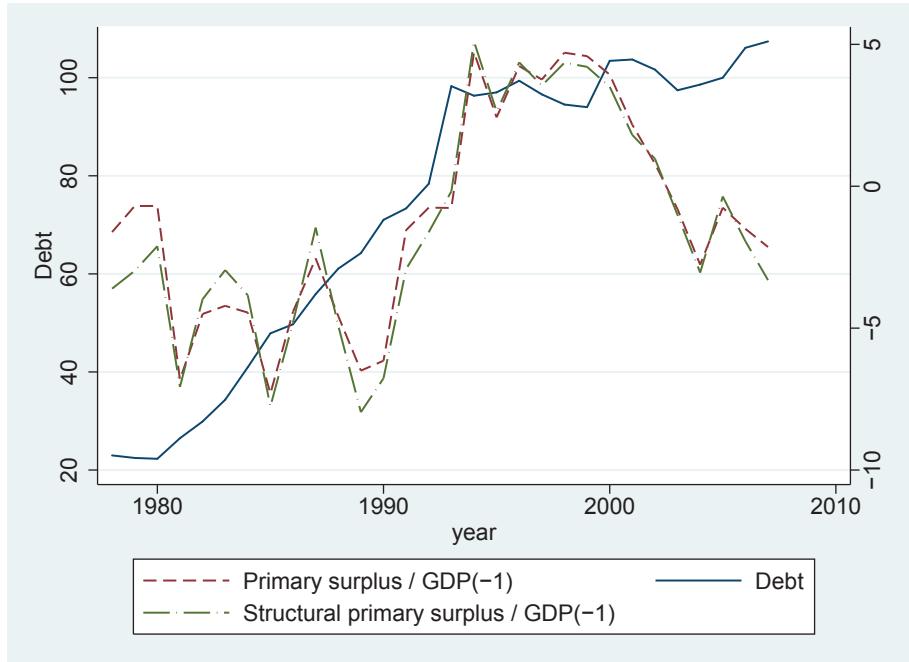


Figure 2: Greek debt, primary and structural primary surpluses over 1978-2007 (% of GDP). Data are taken from the AMECO (March 2011) database. Over 1995-2007, they correspond to those published by Eurostat in February 2012.

### III.2 Estimation of a fiscal reaction function when primary surplus and debt are integrated

When primary surplus and public debt are both integrated time series, the fiscal reaction function is a cointegrating relationship. A finite-sample bias might appear if the evolution of the debt / GDP ratio is correlated to the primary surplus / GDP ratio (*cf.* III.3). To eliminate this bias, Stock and Watson (1993) recommend to include leads and lags of public debt's variation in the regression:

$$\frac{S_t}{Y_{t-1}} = \alpha + \beta \frac{D_{t-1}}{Y_{t-1}} + \sum_{i=-n}^n \gamma_i \left( \frac{D_{t+i-1}}{Y_{t+i-1}} - \frac{D_{t+i-2}}{Y_{t+i-2}} \right) + \mu_t \quad (4)$$

### III.3 Estimation of a fiscal reaction function when primary surplus and debt are both stationary, the latter being much more persistent than the former

The following regression has to be estimated (*cf. supra* for date conventions):

$$\frac{S_t}{Y_{t-1}} = \alpha + \beta \frac{D_{t-1}}{Y_{t-1}} + \mu_t$$

Results of this regression are difficult to interpret when the primary surplus/GDP ratio is stationary and the debt/GDP ratio is also stationary but very persistent.<sup>15</sup>

---

<sup>15</sup>We assume from the start that unit-root tests do not allow us to differentiate between a formally integrated and a very persistent series for usual sample sizes. If one is absolutely sure to regress a stationary series on an integrated one, the true value of the  $\beta$  coefficient cannot be different from

This is a pure econometric issue, not an economic one.

First of all, suppose that the regressor is formally I(1). The error term  $\mu_t$  is most likely correlated with the evolution of the debt/GDP ratio between the end of period  $t - 1$  and the end of period  $t$ . Indeed, an increase in primary surplus leads to a decrease in debt, everything else held equal. In such a case, the estimator  $\hat{\beta}$  has a non-standard asymptotic distribution and a finite-sample bias. The bias is present even when the regressor is predetermined as it is in our case. Thus, it is not a simultaneity bias. Despite the superconvergence property of the estimator, this finite-sample bias is particularly impeding for samples of standard sizes and can lead us to over-reject  $H_0$  ( $\beta = 0$ ) using a Student test with usual critical values.

With a finite sample, the same difficulty arises for time series that are not formally integrated but simply very persistent (cf. Mankiw and Shapiro (1986) for an empirical illustration and Banerjee and Dolado (1988) for a theoretical explanation). The sign and the size of this bias depend on the unknown correlation between the error term and the evolution of the debt/GDP ratio.

The existence of this bias casts doubt on the results obtained from panel regressions with numerous countries having a persistent debt/GDP ratio such as in Mendoza and Ostry (2008) and the study by the European Commission (PFR 2011).

A first way to eliminate the finite sample bias would be to add an additional lag of the debt/GDP ratio in the regression (3), which gives:

$$\frac{S_t}{Y_{t-1}} = \alpha + \beta \frac{D_{t-1}}{Y_{t-1}} + \gamma \frac{D_{t-2}}{Y_{t-2}} + \mu_t \quad (5)$$

Even when the debt ratio is integrated, estimators  $\hat{\beta}$  and  $\hat{\gamma}$  converge in  $\sqrt{T}$  to standard normal distributions centered at  $\beta$  and  $\gamma$ . Indeed, regression (5) can be rewritten differently with these coefficients associated with stationary variables. We use the fact that the difference  $\frac{D_{t-1}}{Y_{t-1}} - \frac{D_{t-2}}{Y_{t-2}}$  is stationary. It is a direct application of a theorem by Sims, Stock and Watson (1990). Simulations done by Galbraith and al. (1987) show that using this method yields excellent results in the case of regressors that are not formally integrated processes but only very persistent.

This parametric method could solve the aforementioned econometric problems due to heterogeneous persistence, but we will not rely on it in the present context for two reasons. First, it would require to make strong assumptions on the stochastic properties of the debt to GDP ratio (e.g.: bounded process) to comply with the proof given in appendix if  $\frac{D_{t-2}}{Y_{t-2}}$  is considered as a control variable. Second, it is not obvious to extend Bohn's proof to the case of fiscal reaction functions with lags of the debt/GDP ratio and/or additional lags of the surplus/GDP ratio. Computations become extremely cumbersome in this case.<sup>16</sup>

---

zero so that the hypothesis on the existence of a fiscal reaction function would have to be rejected. Therefore, we do not rely on econometric estimations when surplus and debt have different orders of integration.

<sup>16</sup>Notice that this difficulty is never taken into account in the empirical literature estimating fiscal reaction functions. In particular, Mendoza and Ostry (2008) only report estimation results with an AR(1) residual. The fact that a significantly positive reaction of primary surplus to indebtedness implies sustainability in this case is not proven.

### III.4 Non-parametric tests

The problem arising from the correlation between primary surplus innovations and future values of debt can also be solved using non-parametric tests, without additional lags in the equation. According to Campbell and Dufour (1997), if  $\frac{S_t}{Y_{t-1}}$  is independent from the past (in particular from  $\frac{D_{t-1}}{Y_{t-1}}$  under the null hypothesis  $\beta = 0$ ) and has a median  $b_0$ , then the finite-sample exact distribution of the sign statistic  $S_g(b_0) = \sum_{t=1}^n u[(\frac{S_t}{Y_{t-1}} - b_0)(\frac{D_{t-1}}{Y_{t-1}} - \hat{m}_{t-1})]$  is known, where  $u(z) = 1$  if  $z \geq 0$  and  $u(z) = 0$  if  $z < 0$ , and  $\hat{m}_{t-1}$  is the empirical median of the first  $t - 1$  observations of the debt ratio. Moreover, if the primary surplus ratio has a continuous and symmetric distribution about  $b_0$ , then we also know the exact distribution of the *signed rank* statistic  $SR_g(b_0) = \sum_{t=1}^n u[(\frac{S_t}{Y_{t-1}} - b_0)(\frac{D_{t-1}}{Y_{t-1}} - \hat{m}_{t-1})]R_t^+(b_0)$  where  $R_t^+(b_0)$  denotes the rank of  $|\frac{S_t}{Y_{t-1}} - b_0|$  among  $|\frac{S_1}{Y_0} - b_0|, \dots, |\frac{S_{n-1}}{Y_{n-2}} - b_0|$  sorted in ascending order, that is  $R_t^+(b_0) = \sum_{j=1}^n u[|\frac{S_t}{Y_{t-1}} - b_0| - |\frac{S_j}{Y_{j-1}} - b_0|]$ .

Both tests rely on the comparison of the signs of  $\frac{S_t}{Y_{t-1}} - b_0$  and  $\frac{D_{t-1}}{Y_{t-1}} - \hat{m}_{t-1}$ . If  $\beta$  is positive, both primary surplus and debt will tend to be above or below their median at the same time, meaning that  $(\frac{S_t}{Y_{t-1}} - b_0)(\frac{D_{t-1}}{Y_{t-1}} - \hat{m}_{t-1})$  will be more frequently positive than negative. In such a case, the sign statistic  $S_g(b_0)$  and the signed rank statistic  $SR_g(b_0)$  will be positive and far from 0. In contrast with a negative  $\beta$ ,  $\frac{S_t}{Y_{t-1}} - b_0$  and  $\frac{D_{t-1}}{Y_{t-1}} - \hat{m}_{t-1}$  will generally display opposite signs, entailing sign and signed rank statistics near 0.

When the median  $b_0$  of the primary surplus ratio is unknown, Campbell and Dufour (1997) propose two strategies. The first strategy consists in computing the above statistics with the empirical estimator  $\tilde{b}_0$  of the median  $b_0$  on the whole sample. However, finite sample distributions of test statistics are not available in this case. The second strategy consists in three steps: first, an exact confidence interval of level  $\alpha_1$  for  $b_0$  is computed; then, test statistics of level  $\alpha_2$  are computed for each value inside the confidence interval; finally, these statistics are combined with the confidence interval for  $b_0$  using Bonferroni's inequality in order to end up with a finite-sample exact non-parametric test at the desired level  $\alpha_1 + \alpha_2 = \alpha$ .

These non-parametric tests have several advantages compared with the frequently used parametric tests. No restriction is imposed either on the correlation between innovations of the primary surplus ratio and future values of the debt ratio, or on the nature of the innovations generating primary surplus and debt: they can be heteroscedastic and follow non-normal distributions. These tests also rely on exact finite-sample critical values. Numerical simulations done by Campbell and Dufour (1997) show that these test statistics do not wrongly over-reject the null hypothesis and display a power at least similar to standard  $t$ -tests in finite samples.

However, these non-parametric tests are only valid under the assumption that the primary surplus ratio is not autocorrelated under the null hypothesis. This assumption seems to be more acceptable if we consider the cyclically-adjusted (i.e. structural) primary surplus ratio rather than the non-cyclically adjusted primary surplus ratio. Therefore, we only present results of the non-parametric tests when the dependent variable is the structural primary surplus ratio. Notice that this choice amounts to follow Bohn's (1998) advice and to control for the cyclical evolution of the primary

surplus ratio (see III.5). Campbell and Dufour (1997) also suggest a method to take into account autocorrelated innovations by considering two subsamples. The first one only contains observations at even dates and the second one those at odd dates. A test of level  $\alpha/2$  on each of them will actually amount to an  $\alpha$ -level test on the whole sample.

### III.5 Empirical results for France

Fiscal reaction functions are only estimated on the 1978-2007 sample so that national accounts data are definitive and output gap estimates are more reliable. Indeed, the output gap appears to be a potentially important variable determining the primary surplus / GDP ratio and is most likely correlated with the debt to GDP ratio. Bohn (1998) also suggests to include the output gap in the regression. But rather than directly estimating the elasticity of primary surplus to output gap because we would need instrumental variables to do it properly, we rely on the elasticity of 0.5 computed for France by Guyon and Sorbe (2009). We use the output gap computed by the European Commission (AMECO database) rather than an HP filter because the estimate of the European Commission relies on a production function and is therefore more structural. Since most revisions of this series seem to be concentrated on the last 3 or 4 years, the output gap series computed until 2007 is considered to be reliable.

Considering usual stationarity tests (ADF, KPSS and ERS, see Table 1a), both gross and net debt ratios seem to be I(1) whereas the cyclically-unadjusted primary surplus ratio seems to be I(0). However, the KPSS and ERS unit-root tests lead to inconclusive results for the structural primary surplus. Since we consider that it is not possible for these tests to distinguish between formally integrated series and stationary but very persistent series with the available data, we will assume first that both primary surplus ratios and the net debt ratios are formally I(1), and then that all these variables are stationary with possibly high persistence.<sup>17</sup>

First considering that all series are I(1), we apply the Stock and Watson (1993) method to estimate the fiscal reaction function for France. Results are presented in Table 2. The coefficient on the debt to GDP ratio is never significant. A Shin (1994) test does not reject the cointegration hypothesis between debt and the primary surpluses.<sup>18</sup>

If we assume now that the cyclically-adjusted primary surplus and net financial debt ratios are stationary but the latter very persistent, we apply non-parametric tests introduced by Campbell and Dufour (1997) to implement the sustainability analysis. Specification (3) is used and right unilateral tests are computed. The significance of the fiscal reaction coefficient is assessed at a level of 5%. Sign and signed-rank statistics are computed using either the empirical median estimate of the structural primary surplus ratio (median-estimate tests) or a confidence interval for this median (bounds tests).

Results are reported in Table 1b. Using the empirical median estimate on the sample, the null hypothesis cannot be rejected: the  $p$ -value is 0.64% for the sign

---

<sup>17</sup>Remember that we only consider cases where surplus and debt have the same order of integration. If they have different orders of integration, the true value of  $\beta$  can only be 0.

<sup>18</sup>KPSS statistics for the residuals of regression (1) to (4) of Table 2 are respectively 0.073, 0.058, 0.102 and 0.104 to be compared with Shin (1994) asymptotic critical value at 10 % of 0.231.

Variable	Order of integration	Level		1st difference
		ADF	KPSS	ERS
$S/GDP(-1)$	0	-3.11**	0.13	0.79***
$S \text{ struct}/GDP(-1)$	0/1	-2.49	0.17	-4.26**
$D_{net}/GDP$	1	-1.58	0.64†	-5.75**
$D_{gross}/GDP$	1	-0.64	0.67†	0.26
			95.60	-3.43**
				0.12
				0.31***

Table 1a: France 1978-2007. Order of integration of fiscal variables with t-stat. \*\*\*(\*\*\*) indicates rejection of the null hypothesis of non-stationarity (ADF, ERS) at a 1% (5%, 10%) level and †††(††, †) rejection of the null of stationarity (KPSS) at a 1% (5%, 10%) level

$S \text{ struct}/GDP(-1)$	Median-Estimate Tests				Bound Tests			
	$Sg$	Interpretation	$SRg$	Interpretation	$SB$	Interpretation	$SRB$	Interpretation
Total sample	0.64	$H_0$ not rejected	0.66	$H_0$ not rejected	$Q_L$	$Q_U$		
Sub-sample A	0.40	$H_0$ not rejected	0.64	$H_0$ not rejected	0.97	0.03		
Sub-sample B	0.21	$H_0$ not rejected	0.24	$H_0$ not rejected	0.91	0.00		
					0.79	0.01		

Table 1b: France 1978-2007. Under  $H_0$ , primary surplus ratios and debt ratios are independent. Right unilateral tests are performed on the statistics  $Sg$ ,  $SRg$ ,  $SB$  and  $SRB$ .  $p$ -values are indicated in the table.  $Q_L$  is the smallest value taken by the test statistic on the confidence interval defined for  $b_0$ .  $Q_U$  is the largest value

Note : For median-estimate tests, relying on the empirical median estimate  $b_0$  of the structural primary surplus / GDP(-1) ratio, significance is tested at a 5% level (2.5% for the subsamples).

For bounds tests, a 99% confidence interval  $J(0.01)$  is first constructed for the median  $b_0$  on the whole sample (99.5% on each subsample).  $H_0$  is rejected if, for all  $b \in J(0.01)$  ( $J(0.005)$  for subsamples), the test statistic is above the 4% critical value (2% for subsamples).  $H_0$  is not rejected if, for all  $b \in J(0.01)$  ( $J(0.005)$  for subsamples), the test statistic is less than the 6% critical value (3% for subsamples). It may occur that  $Q_L$  is less than the 4% (2%) critical value but that  $Q_U$  is above the 6% (3%) critical value. In this case, test results are said to be inconclusive.

	(1) $S/GDP(-1)$	(2) $S/GDP(-1)$	(3) $S \text{ struct}/GDP(-1)$	(4) $S \text{ struct}/GDP(-1)$
$D(-1)/GDP(-1)$	0.0196 (0.0143)	0.0203 (0.0151)	-0.0131 (0.0175)	-0.0126 (0.0165)
$D(+1)/GDP(+1) - D/GDP$	-0.0473 (0.0582)		-0.0515 (0.0698)	
$D/GDP - D(-1)/GDP(-1)$		-0.136 (0.0849)	-0.145* (0.0765)	-0.110* (0.0587)
$D(-1)/GDP(-1) - D(-2)/GDP(-2)$		-0.133** (0.0576)	-0.0907 (0.0583)	-0.000308 (0.0777)
$D(-2)/GDP(-2) - D(-3)/GDP(-3)$		-0.116 (0.0713)	-0.0827 (0.0780)	-0.00972 (0.0767)
$D(-3)/GDP(-3) - D(-4)/GDP(-4)$		-0.0243 (0.0575)	0.0491 (0.0532)	0.0213 (0.0636)
Constant	-0.624 (0.446)	-0.914** (0.360)	-0.469 (0.417)	-0.502 (0.379)
Observations	25	27	25	27
Adjusted $R^2$	0.460	0.428	0.005	0.020

Standard errors in parentheses

\*  $p < 0.10$ , \*\*  $p < 0.05$ , \*\*\*  $p < 0.01$

Table 2: France 1978-2007. OLS estimates with Newey-West standard errors

statistic and 0.66% for the signed-rank statistic. Using a confidence interval for the median of the structural primary surplus ratio, the null hypothesis is not rejected either (cf. details under Table 1b). Like Campbell and Ghysels (1995), we then divide the sample in two parts and apply the same non-parametric tests on each subsample so that the assumption of non-autocorrelated residuals becomes more credible. Under the null hypothesis, this assumption means that structural primary surplus ratios are non-autocorrelated in each subsample. These robustness checks confirm our previous results, indicating a lack of response of primary surplus to indebtedness.

We then perform the same analysis with quarterly data interpolated from the annual national accounts, yielding similar results. Table 3a shows stationarity tests for these fiscal variables, indicating that net debt and both surplus ratios are I(1) and cointegrated. Applying once again the Stock and Watson (1993) method leads to the same conclusion for French debt sustainability: no evidence of a significantly positive fiscal reaction function, as reported in Table 3b.

As a conclusion for the French case, results of parametric and non-parametric tests are mitigated but they do not indicate a significantly positive fiscal reaction function in the past.<sup>19</sup> So, to the extent private investors used the fiscal reaction function as a device to assess sustainability, they probably anticipated a strengthening of the fiscal reaction even before the start of the financial crisis to justify their buying of French public debt. However, French public debt continued to increase after the end of the estimation sample and French borrowing costs remained low, or even very low.

### III.6 Empirical results for Greece

Debt and primary surplus ratios may be both considered as I(1) for this country. Therefore, the fiscal reaction function is estimated using Stock and Watson (1993) method. Results are presented in Table 4b. The coefficient on the debt to GDP ratio is estimated at around 0.1 for the 1978-2007 period, depending on the specification. It is always significant at a 1% level. This estimate is very high, implying that a 10 points increase in the debt ratio leads to a 1 point increase in the (structural) primary surplus, thus pointing strongly towards sustainability. A Shin (1994) test does not reject the cointegration hypothesis between (structural) primary surplus and debt ratios.<sup>20</sup> Notice that Greece also appears as a country with very sustainable public finances in Mendoza and Ostry (2008) who also estimate fiscal reaction functions.

Of course, this result may seem confusing when one considers the recent economic developments in Greece. This should be an important warning for the users of econometric sustainability tests. Greece is actually unable to finance its public debt on the market although its past fiscal reaction function points to a sustainable indebtedness. In fact, investors probably anticipated that Greece would be unable to apply this fiscal reaction function at higher debt levels. This is exactly the issue that Bi and Leeper (2012) deal with using a general equilibrium model. Their conclusion

---

<sup>19</sup>The estimation of a fiscal reaction function for Germany is not considered in this paper. Indeed the huge challenges following the German reunification probably caused a break in the fiscal reaction function. Furthermore the treatment of the privatizations of eastern companies in the early 1990's through the Treuhandanstalt should be taken into account.

<sup>20</sup>KPSS statistics for the residuals in regressions (1) to (4) of Table 4b are respectively 0.117, 0.121, 0.104 and 0.112, the Shin (1994) asymptotic critical value at 10% being 0.231.

Variable	Order of integration	ADF	Level KPSS	ERS	1st difference
$S/GDP(-1)$	1	-2.13	0.20	7.30	-14.18***
$S \text{ struct}/GDP(-1)$	1	-2.68*	0.18	9.87	-14.68***
$D_{net}/GDP$	1	-1.69	1.12 † †	31.87	-3.70***

Table 3a: France 1980Q1-2007Q4. Order of integration of quarterly fiscal variables with t-stat. \*\*\* (\*\*\*,\*) indicates rejection of the null hypothesis of non-stationarity (ADF,ERS) at a 1% (5%,10%) level and ††(††,†) rejection of the null of stationarity (KPSS) at a 1% (5%, 10%) level

	(1) $S/GDP(-1)$	(2) $S/GDP(-1)$	(3) $S \text{ struct}/GDP(-1)$	(4) $S \text{ struct}/GDP(-1)$
$D(-1)/GDP(-1)$	0.003 (0.003)	0.003 (0.002)	-0.003 (0.003)	-0.003 (0.003)
$D(+1)/GDP(+1) - D/GDP$	0.005 (0.079)	0.005 (0.079)	-0.036 (0.0634)	
$D/GDP - D(-1)/GDP(-1)$	-0.206*** (0.069)	-0.182** (0.072)	-0.143** (0.066)	-0.188 (0.061)
$D(-1)/GDP(-1) - D(-2)/GDP(-2)$	0.078 (0.056)	0.100 (0.062)	0.083 (0.058)	0.094 (0.058)
$D(-2)/GDP(-2) - D(-3)/GDP(-3)$	-0.010 (0.064)	-0.158 (0.074)	-0.027 (0.054)	-0.027 (0.070)
$D(-3)/GDP(-3) - D(-4)/GDP(-4)$	-0.130 (0.080)	-0.003 (0.002)	-0.003 (0.071)	
Constant	-0.008*** (0.002)	-0.008*** (0.002)	-0.004 (0.003)	-0.004 (0.003)
Observations	107	109	107	109
Adjusted $R^2$	0.42	0.41	0.12	0.15

Standard errors in parentheses

\*  $p < 0.10$ , \*\*  $p < 0.05$ , \*\*\*  $p < 0.01$

Table 3b: France 1980Q1-2007Q4. OLS estimates with Newey-West standard errors.  $D$  denotes the French general government net debt

Variable	Order of integration	ADF	Level KPSS	ERS	1st difference
$S/GDP(-1)$	1	-1.68	0.31	4.61	-6.05***
$S \text{ struct}/GDP(-1)$	1	-1.79	0.33	4.74	-5.67***
$D/GDP$	1	-1.36	0.66 ††	158.86	-4.71***
=					0.25

Table 4a: Greece 1978-2007. Order of integration of fiscal variables with t-stat. \*\*\* (\*\*\*, †) indicates rejection of the null hypothesis of non-stationarity (ADF, ERS) at a 1% (5%, 10%) level and ††(††, †) rejection of the null of stationarity (KPSS) at a 1% (5%, 10%) level

	(1) $S/GDP(-1)$	(2) $S/GDP(-1)$	(3) $S \text{ struct}/GDP(-1)$	(4) $S \text{ struct}/GDP(-1)$
$D(-1)/GDP(-1)$	0.112*** (0.0273)	0.102*** (0.0218)	0.103*** (0.0333)	0.0966*** (0.0260)
$D(+1)/GDP(+1) - D/GDP$	0.0158 (0.0708)	-0.0272 (0.0732)		
$D/GDP - D(-1)/GDP(-1)$	-0.0634 (0.110)	-0.0623 (0.0914)	-0.0580 (0.113)	-0.0502 (0.0973)
$D(-1)/GDP(-1) - D(-2)/GDP(-2)$	0.0604 (0.131)	0.0229 (0.134)	0.0488 (0.151)	0.0144 (0.153)
$D(-2)/GDP(-2) - D(-3)/GDP(-3)$	-0.0267 (0.107)	-0.0130 (0.100)	-0.0217 (0.111)	-0.00514 (0.103)
$D(-3)/GDP(-3) - D(-4)/GDP(-4)$	0.0494 (0.101)	0.0487 (0.108)		
Constant	-9.577*** (2.626)	-8.675*** (1.633)	-8.857** (3.290)	-8.487*** (2.116)
Observations	25	27	25	27
Adjusted $R^2$	0.470	0.506	0.356	0.396

Standard errors in parentheses  
\*  $p < 0.10$ , \*\*  $p < 0.05$ , \*\*\*  $p < 0.01$

Table 4b: Greece 1978-2007. OLS estimates with Newey-West standard errors

is that the default risk does not only depend on a fiscal reaction function but also on the fact that the product of taxes cannot grow indefinitely to stabilize debt above a certain threshold due to economic and social constraints (Laffer curve). It is also possible that the 2000's increase in the share of foreign holders of public debt has changed the fiscal reaction function or the reaction of the market to new developments in public finance. Given that our analysis uses the most accurate data as of 2012 for the period 1978-2007, it is very likely that the same analysis with 2007 data would have pointed even more strongly towards sustainability. Yet the uncovering of the misleading fiscal figures in 2010 certainly undermined the investors' confidence in the Greek government, their statistics and their ability to react according to the estimated fiscal reaction function.

## Conclusion

This paper has recalled the weaknesses associated with the first generation of sustainability tests in public finance. Some of them can be overcome using Bohn's suggestion to estimate fiscal reaction functions linking primary surplus and public debt. A positive link is a sufficient sustainability condition, under the strong condition that the control variables and the error term are bounded. In practice, since this method also entails econometric difficulties when primary surplus and debt have a very different persistence or are both integrated, we have put forward parametric and non-parametric methods in order to deal with these issues.

But even the second generation of sustainability tests has strong empirical limitations, as we have shown using French and Greek national accounts over the last 30 years. Because Greece generated an enormous increase of its primary surplus during the 1990s, it appears to fulfill this sufficient sustainability condition in 2007. This result is clearly at odds with recent economic developments in this country. As for France, results of parametric and non-parametric sustainability tests do not indicate a significantly positive fiscal reaction function over the years 1978-2007. Again, this result is at odds with subsequent developments. Indeed, French public debt has increased markedly after the end of the estimation sample, investors have continued to consider French public indebtedness as sustainable and borrowing costs have remained low, or even very low.

Our results highlight the limits of econometric sustainability tests. Even if they are correctly specified, they only give an answer to the following question: is it rational for an investor, using only the past reaction of primary surplus to debt, to lend money to a government? In fact, fiscal reaction functions can evolve strongly according to the circumstances and the sustainability of a country's public finance depends above all on the quality and strength of its institutions.

## A Appendix

### A.1 Sufficient sustainability condition based on the fiscal reaction function

This appendix gives a theoretical justification for estimating fiscal reaction functions. It is adapted from Bohn's (1998) unpublished appendix. Compared to Bohn's original proof, date conventions have been changed:  $D_t$  is now the end of period  $t$  debt whereas it is the beginning of period  $t$  debt in Bohn (1998) and the interest rate on a loan made in period  $t$  is  $R_t$  instead of  $R_{t+1}$ . We also divide primary surplus  $S_t$  and debt  $D_t$  by the GDP of period  $(t-1)$   $Y_{t-1}$  (see III for an econometric justification, related to the estimation of the fiscal reaction function). Finally, the public debt accumulation equation becomes:  $D_t = (D_{t-1} - S_t)(1 + R_t)$ . This accounting equation means that debt at the end of period  $t$  already includes the interest burden that is due for period  $(t+1)$ . In period  $t$ , households lend  $D_{t-1} - S_t$  to the government and will be repaid  $(D_{t-1} - S_t)(1 + R_t)$  in period  $(t+1)$ . As a consequence, the equation linking the households' stochastic discount factor and the risk-free interest rate on public debt is  $\mathbb{E}_t [u_{t+i,1} \cdot (1 + R_{t+i})] = 1$ .

The debt accumulation equation can be divided by the GDP of period  $t$ :

$$d_t \equiv \frac{D_t}{Y_t} = \left( \frac{D_{t-1}}{Y_{t-1}} - \frac{S_t}{Y_{t-1}} \right) \cdot (1 + R_t) \frac{Y_{t-1}}{Y_t} \equiv \left( \frac{D_{t-1}}{Y_{t-1}} - \frac{S_t}{Y_{t-1}} \right) \cdot x_t$$

Suppose that the fiscal reaction function is of the following form, with  $0 < \rho < 1$ :

$$s_t \equiv \frac{S_t}{Y_{t-1}} = \rho \frac{D_{t-1}}{Y_{t-1}} + \mu_t$$

Like in Bohn (1998),  $\mu_t$  comprises control variables and a structural error term.

Primary surplus can then be taken out of the equation governing the evolution of public debt. By successive iterations, we get:

$$d_{t+n} = \left( \prod_{j=1}^n x_{t+j} \right) (1 - \rho)^n d_t - \sum_{i=1}^n \left( \prod_{j=i}^n x_{t+j} \right) (1 - \rho)^{n-i} \mu_{t+i}$$

We can note that this equation implicitly assumes that there is no default, which underlies the only additional technical assumption that we need compared to Bohn (1998): the interest rate  $R_t$  is bounded, i.e.  $0 < m \leq 1 + R_t \leq M$ . This implies, given the positivity of  $u_{t+i,1}$ , that:  $m u_{t+i,1} \leq u_{t+i,1}(1 + R_{t+i}) \leq M u_{t+i,1} \Rightarrow \frac{1}{M} \leq \mathbb{E}_t[u_{t+i,1}] \leq \frac{1}{m}$ .

We deduce in the next steps:

$$\begin{aligned} \frac{\mathbb{E}_t [u_{t,n} \cdot D_{t+n}]}{Y_t} &= \mathbb{E}_t \left[ u_{t,n} \cdot \prod_{j=1}^n (1 + y_{t+j}) \cdot d_{t+n} \right] \\ &= (1 - \rho)^n \cdot \mathbb{E}_t \left[ u_{t,n} \cdot \prod_{j=1}^n (1 + y_{t+j}) \cdot \prod_{j=1}^n x_{t+j} \right] \cdot d_t \\ &\quad - \sum_{i=1}^n (1 - \rho)^{n-i} \cdot \mathbb{E}_t \left[ u_{t,n} \cdot \prod_{j=1}^n (1 + y_{t+j}) \cdot \prod_{j=i}^n x_{t+j} \cdot \mu_{t+i} \right] \end{aligned}$$

$$\begin{aligned}
&= (1 - \rho)^n \cdot \mathbb{E}_t \left[ u_{t,n} \cdot \prod_{j=1}^n (1 + R_{t+j}) \right] \cdot d_t \\
&\quad - \sum_{i=1}^n (1 - \rho)^{n-i} \cdot \mathbb{E}_t \left[ u_{t,n} \cdot \prod_{j=i}^n (1 + R_{t+j}) \cdot \prod_{j=1}^{i-1} (1 + y_{t+j}) \cdot \mu_{t+i} \right] \\
&= (1 - \rho)^n \cdot \mathbb{E}_t \left[ u_{t,1} \prod_{j=1}^{n-1} u_{t+j,1} \cdot (1 + R_{t+j}) (1 + R_{t+n}) \right] \cdot d_t \\
&\quad - \sum_{i=1}^n (1 - \rho)^{n-i} \cdot \mathbb{E}_t \left[ u_{t,i} \cdot \prod_{j=1}^{i-1} (1 + y_{t+j}) \cdot \prod_{j=i}^{n-1} u_{t+j,1} \cdot (1 + R_{t+j}) \cdot (1 + R_{t+n}) \cdot \mu_{t+i} \right]
\end{aligned}$$

We then use the law of iterated expectations and give an upper bound to the absolute value of  $\frac{\mathbb{E}_t[u_{t,n} \cdot D_{t+n}]}{Y_t}$ . Indeed, all the terms in the integrands except  $\mu_t$  are positive and we assume, like Bohn (1998), that the process  $\mu_t$  is bounded, meaning that there exists a  $M_0$  such that the realization of  $\mu_t$  in every state of nature and at each date lies between  $-M_0$  and  $M_0$ . Therefore:

$$\begin{aligned}
\left| \frac{\mathbb{E}_t[u_{t,n} \cdot D_{t+n}]}{Y_t} \right| &\leq (1 - \rho)^n \cdot d_t \cdot \frac{M}{m} \\
&\quad + \sum_{i=1}^n (1 - \rho)^{n-i} \cdot \mathbb{E}_t \left[ u_{t,i} \cdot \prod_{j=1}^{i-1} (1 + y_{t+j}) \cdot u_{t+i,1} \cdot (1 + R_{t+i}) \cdot |\mu_{t+i}| \right] M \\
&\leq (1 - \rho)^n \cdot d_t \frac{M}{m} + MM_0 \sum_{i=1}^n (1 - \rho)^{n-i} \cdot \mathbb{E}_t \left[ u_{t,i} \cdot \prod_{j=1}^{i-1} (1 + y_{t+j}) \cdot u_{t+i,1} \cdot (1 + R_{t+i}) \right] \\
&\leq (1 - \rho)^n \cdot d_t \frac{M}{m} + MM_0 \sum_{i=1}^n (1 - \rho)^{n-i} \cdot \mathbb{E}_t \left[ u_{t,i-1} \cdot u_{t+i-1,1} \cdot \prod_{j=1}^{i-1} (1 + y_{t+j}) \right] \\
&\leq (1 - \rho)^n \cdot d_t \frac{M}{m} + \frac{M}{m} M_0 \sum_{i=1}^n (1 - \rho)^{n-i} \cdot \mathbb{E}_t \left[ u_{t,i-1} \cdot \prod_{j=1}^{i-1} (1 + y_{t+j}) \right]
\end{aligned}$$

By assumption, also made by Bohn (1998), the discounted value of future revenues

$$\sum_{k=1}^n Y_t \cdot \mathbb{E}_t \left[ u_{t,k} \cdot \prod_{j=1}^k (1 + y_{t+j}) \right] \text{ is finite, so that } \lim_{k \rightarrow +\infty} \mathbb{E}_t \left[ u_{t,k} \cdot \prod_{j=1}^k (1 + y_{t+j}) \right] = 0.$$

It is then straightforward to show that:

$$\lim_{n \rightarrow +\infty} \frac{\mathbb{E}_t[u_{t,n} \cdot D_{t+n}]}{Y_t} = 0$$

This means that the existence of the postulated fiscal reaction function is sufficient for the transversality condition to hold, whatever the exact form of the stochastic discount factor. Recall that this result is valid under some technical assumptions: the control variables and the error term are bounded, the discounted value of future revenues is finite and the interest rate is bounded.

## A.2 Stationarity of the error term and the control variables is not sufficient

It is important to bear in mind that stationarity of the control variables and the error term in the fiscal reaction function together with the positivity of the coefficient on debt is not a sufficient sustainability condition (i.e.: it does not imply the transversality condition (TC)). However, if the control variables and the error term are bounded and if there is a positive  $\beta$  in the fiscal reaction function, then (TC) holds. Weaker conditions on the control variables could be found, but neither boundedness in probability (which is implied by weak stationarity), nor weak stationarity, nor even strong stationarity are sufficient. An example with a weakly stationary process is given below, for which having a positive  $\beta$  in the fiscal reaction function does not imply (TC). Another example with a strongly stationary process follows.

### A.2.1 An example with weak stationarity

Let  $u_k \sim_{iid} U([0, 1])$ . We define  $\mu_k$  and  $u_{t,k} \prod_{j=1}^k (1 + y_{t+j}) \equiv X_k$  as follows:

$$\mu_k = \begin{cases} \sqrt{k^4 - 1} & \text{if } u_k < \frac{1}{k^4} \\ \frac{-1}{\sqrt{k^4 - 1}} & \text{otherwise} \end{cases} \quad X_k = \begin{cases} k^2 & \text{if } u_k < \frac{1}{k^4} \\ 0 & \text{otherwise} \end{cases}$$

It is straightforward to show that  $\mu_k$  is weakly stationary:  $\mathbb{E}[\mu_k] = \frac{\sqrt{k^4 - 1}}{k^4} - \frac{1}{\sqrt{k^4 - 1}} (1 - \frac{1}{k^4}) = 0$ ,  $\mathbb{V}[\mu_k] = \frac{k^4 - 1}{k^4} + \frac{1}{k^4 - 1} (1 - \frac{1}{k^4}) = 1$ , and all the autocorrelations are null given that  $u_k$  is *iid*. Thus,  $\mu_k$  is a weakly stationary process.

Furthermore  $\mathbb{E}[X_k] = \frac{k^2}{k^4} \xrightarrow[k \rightarrow +\infty]{} 0$ .

However,  $\mathbb{E}[X_k \mu_k] = \frac{k^2 \sqrt{k^4 - 1}}{k^4} \xrightarrow[k \rightarrow +\infty]{} 1$ .

In a nutshell, even in taking Bohn's (1998) date conventions and definition of the fiscal reaction function, assuming only that  $\lim_{k \rightarrow +\infty} \mathbb{E}_t \left[ u_{t,k} \cdot \prod_{j=1}^k (1 + y_{t+j}) \right] = 0$  and that  $\mu_t$  is a weakly stationary process does not imply that  $\lim_{k \rightarrow +\infty} \mathbb{E}_t \left[ u_{t,k} \cdot \prod_{j=1}^k (1 + y_{t+j}) \cdot \mu_{t+k} \right] = 0$ , which is essential for the proof to work.

### A.2.2 An example with strong stationarity

Let  $u_k \sim_{iid} U([0, 1])$  and  $\mu_k = -\ln(u_k)$ , defined almost everywhere with mean and variance 1. Since its mean and variance exist, the strongly stationary  $\mu_k$  is also weakly stationary.

Let  $X_k \equiv \frac{1}{k^2 u_k (\ln(u_k) - 1)^2}$ . Then, using a generalized integral:

$$\mathbb{E}_t[X_k] = \frac{1}{k^2} \int_0^1 \frac{du}{u(\ln u - 1)^2} = \frac{1}{k^2} \left[ \frac{-1}{\ln u - 1} \right]_0^1 = \frac{1}{k^2} \xrightarrow[k \rightarrow +\infty]{} 0$$

But  $\forall k \in \mathbb{N}^*$ ,  $\mathbb{E}[X_k \mu_k] = +\infty$ . Indeed for  $0 < a < 1$ , we have:

$$\int_a^1 \frac{-\ln u du}{u(\ln u - 1)^2} = \left[ \frac{\ln u}{\ln u - 1} \right]_a^1 - \int_a^1 \frac{du}{u(\ln u - 1)} = \left[ -\frac{\ln a}{\ln a - 1} \right] - [\ln(1 - \ln u)]_a^1 \xrightarrow[a \rightarrow 0^+]{} +\infty$$

With these  $\mu_k$  and  $u_{t,k} \prod_{j=1}^k (1 + y_{t+j}) = X_k$  processes, the transversality condition is therefore violated. Of course this example remains valid with both Bohn's and our notations for debt and surplus ratios.

### A.3 Debt cannot be at the same time $I(m)_{m \geq 0}$ in level and $I(k)_{k \geq 0}$ after discounting

If  $X_t \sim I(m)$  and  $X_0$  is known, then  $\mathbb{V}[X_t] \sim O(t^{2m})$ . This result can be shown by induction, the assertion being trivial for  $m = 0$ . Let us assume the result established for every  $k < m$ , and let us consider a process  $X_t \sim I(m)$ . The process  $Y_t = (1 - L)X_t$  can then be defined and it is  $I(m - 1)$ . The variance of  $X_t = X_0 + Y_t + \dots + Y_1$  equals  $\sum_{j=1}^t \mathbb{V}[Y_j] + \sum_{j_1, j_2=1, j_1 \neq j_2}^t \text{Cov}[Y_{j_1}, Y_{j_2}]$ . The first term is a sum over  $1 \leq j \leq t$  of  $O(j^{2m-2})$  terms thanks to the induction hypothesis, so it is  $O(t^{2m-1})$ . The second term, with Cauchy-Schwarz inequality, is a sum on  $1 \leq j_1 \neq j_2 \leq t$  of  $O(j_1^{m-1} j_2^{m-1})$  terms, thus is  $O(t^{2m})$ . Eventually we did prove that the variance of the process  $X_t$  is  $O(t^{2m})$ .

Furthermore, with  $X_t \sim I(m)$  and  $Y_t \sim I(m')$  for  $m' \leq m$ , Cauchy-Schwarz inequality allows to write  $\text{Cov}[X_t, Y_t] = O(t^{2m})$ . One can establish by induction on  $k \geq 0$  that there exists coefficients  $\{\alpha_{k,j}\}_{0 \leq j \leq k}$  such that:

$$\Delta^k \left[ \frac{D_{t+n}}{(1+r)^n} \right] = \frac{1}{(1+r)^n} \sum_{j=0}^k \alpha_{k,j} \Delta^j D_{t+n}$$

The  $\{\alpha_{k,j}\}_{0 \leq j \leq k}$  can be obtained by the following recursion:  $\alpha_{k+1,j} = (1+r)\alpha_{k,j-1} - r\alpha_{k,j}$  with  $\alpha_{0,0} = 1$ ,  $\alpha_{k,j} = 0$  for  $j < 0$  and  $j > k$ .

Developing for  $k \geq 0$ :

$$\mathbb{V} \left[ \Delta^k \left[ \frac{D_{t+n}}{(1+r)^n} \right] \right] = \frac{1}{(1+r)^{2n}} \mathbb{V} \left[ \sum_{j=0}^k \alpha_{k,j} \Delta^j D_{t+n} \right]$$

And we notice that the term whose variance we look at is a sum of  $k + 1$  terms all integrated of order smaller or equal than  $m$ . Developing the variance enables to write it as a sum of  $(k + 1) + k(k + 1)$  terms which are all  $O((t + n)^{2m})$ . We can then infer that  $\mathbb{V} \left[ \Delta^k \left[ \frac{D_{t+n}}{(1+r)^n} \right] \right] = O((t + n)^{2m}/(1 + r)^{2n})$ , which means that for every  $k \geq 0$ , this variance will converge towards 0 when  $n$  goes to infinity. Hence, the  $k$  times differentiated discounted debt cannot be a stationary non-zero process for any  $k \geq 0$ .

### A.4 Proof of proposition I.1

**Proposition I.1.** Let  $f$  be a deterministic and discrete function of time.

1. If  $D_{t+n}/f(n) \sim I(m)$ , with  $m \geq 0$  and  $f(n) = o((1+r)^n/n^m)$ , then debt verifies the transversality condition (TC *ad hoc*).
2. If  $D_{t+n}/f(n) \sim I(0)$  with  $f(n) = O((1+r)^n)$  and  $\mathbb{E}[D_{t+n}/f(n)] = 0$ , then debt verifies the transversality condition (TC *ad hoc*).

The proof of the first part is very close to that of proposition 1 in Bohn (2007). Noting  $d_{t+n} = D_{t+n}/f(n)$  and assuming that this process is  $I(m)$ , we can write, with Bohn's notations:

$$d_{t+n} = \sum_{k=0}^{m-1} p_k(n) \Delta^k d_t + \sum_{i=1}^n p_{m-1}(i) \Delta^m d_{t+(n+1-i)}$$

This implies:

$$\mathbb{E}_t[D_{t+n}]/(1+r)^n = \frac{f(n)}{(1+r)^n} \left( \sum_{k=0}^{m-1} p_k(n) \Delta^k d_t + \sum_{i=1}^n p_{m-1}(i) \mathbb{E}_t[\Delta^m d_{t+(n+1-i)}] \right).$$

Since  $\Delta^k d_t$  is known at time  $t$  and  $p_k(n) = O(n^k)$ ,  $\sum_{k=0}^{m-1} p_k(n) \Delta^k d_t = O(n^{m-1})$ .

Moreover,  $\mathbb{E}_t[\Delta^m d_{t+(n+1-i)}] \xrightarrow[n \rightarrow +\infty]{\mathbb{P}} \mu \equiv \mathbb{E}[\Delta^m d_t]$  and  $\sum_{i=1}^n p_{m-1}(i) = O(n^m)$ , implying  $\sum_{i=1}^n p_{m-1}(i) \mathbb{E}_t[\Delta^m d_{t+(n+1-i)}] = O_p(n^m)$ .

Finally,  $\left( \sum_{k=0}^{m-1} p_k(n) \Delta^k d_t + \sum_{i=1}^n p_{m-1}(i) \mathbb{E}_t[\Delta^m d_{t+(n+1-i)}] \right) = O_p(n^m)$ .

Hence,  $\mathbb{E}_t[D_{t+n}]/(1+r)^n \xrightarrow[n \rightarrow +\infty]{\mathbb{P}} 0$ .

The proof of the second part is straightforward noting that  $\lim_{n \rightarrow +\infty} \mathbb{E}_t[D_{t+n}/f(n)] = \mathbb{E}[D_{t+n}/f(n)] = 0$  given the stationarity of  $D_{t+n}/f(n)$ .

## A.5 Description of the French quarterly data

Quarterly data on general government net surplus  $S_t$  (B9A) as well as interest payments<sup>21</sup> are extracted from the quarterly national accounts (base 2000, INSEE). General government quarterly primary surplus can be simply deduced from those two series. The corresponding cyclically-adjusted primary surplus requires the computation of an output gap at the same frequency. We therefore construct a quarterly potential GDP with a quadratic interpolation of the annual potential GDP provided by the European Commission (in base 2005, not available in base 2000). We can then compute a quarterly output gap for France using real quarterly GDP (quarterly national accounts in base 2005 as well). Using the same elasticity of primary surplus with respect to output gap as for annual data (0.5), we obtain a quarterly cyclically-adjusted primary surplus.

General government net financial debt is only published on an annual basis. Its evolution is linked to surplus by the following equation:

$$\Delta D_{net,t} = -S_t + Adj_t$$

where  $Adj_t$  is an adjustment term reflecting revaluation of assets and liabilities in the government balance sheet.

The quarterly evolution of net financial debt can be deduced from the quarterly surplus. Chow and Lin's (1971) method is used to compute the adjustment term at a quarterly frequency under the constraint that debt annual evolution is equal

---

<sup>21</sup>We use net interest paid (D41 paid minus received) to be coherent with our choice of the net debt ratio.

to its 4 quarterly evolutions over the year. Surplus and net financial debt at a quarterly frequency are finally divided by nominal quarterly GDP (same date for debt, previous date for surplus) in order to estimate the fiscal reaction function at a quarterly frequency. Note that the coefficient on debt is therefore divided by about 4.

## References

- [1] A. Banerjee and J. Dolado. Tests of the life cycle-permanent income hypothesis in the presence of random walks: asymptotic theory and small-sample interpretations. *Oxford Economic Papers*, 40(4):610–633, 1988.
- [2] A. Bénassy-Quéré and G. Roussellet. Fiscal sustainability in the presence of systemic banks: the case of eu countries. 2012. Working paper.
- [3] H. Bi and E.M. Leeper. Analyzing fiscal sustainability. 2012. Working paper.
- [4] O.J. Blanchard. Suggestions for a new set of fiscal indicators. *OECD Economics Department Working Papers*, 79, 1990. <http://dx.doi.org/10.1787/435618162862>.
- [5] H. Bohn. The sustainability of budget deficits with lump-sum and with income-based taxation. *Journal of Money, Credit and Banking*, 23(3):580–604, 1991.
- [6] H. Bohn. The sustainability of budget deficits in a stochastic economy. *Journal of Money, Credit and Banking*, 27(1):257–271, 1995.
- [7] H. Bohn. The behavior of US public debt and deficits. *Quarterly Journal of Economics*, 113(3):949–963, 1998.
- [8] H. Bohn. Are stationarity and cointegration restrictions really necessary for the intertemporal budget constraint? *Journal of Monetary Economics*, 54:1837–1847, 2007.
- [9] J. Boissinot, C. L’Angevin, and B. Monfort. Public debt sustainability: some results on the French case, 2004. Document de travail de la Direction des Etudes et Synthèses Economiques, INSEE N°2004/10.
- [10] B. Bourges. La dette des administrations publiques au sens de Maastricht et sa cohérence avec les comptes financiers, 2007. Note méthodologique N°6 des comptes nationaux en base 2000.
- [11] B. Campbell and J.M. Dufour. Over-rejections in rational expectations models: A non-parametric approach to the mankiw-shapiro problem. *Economics Letters*, 35(3):285–290, 1991.
- [12] B. Campbell and J.M. Dufour. Exact nonparametric orthogonality and random walk tests. *The Review of Economics and Statistics*, pages 1–16, 1995.
- [13] B. Campbell and J.M. Dufour. Exact nonparametric tests of orthogonality and random walk in the presence of a drift parameter. *International Economic Review*, pages 151–173, 1997.
- [14] B. Campbell and E. Ghysels. Federal budget projections: A nonparametric assessment of bias and efficiency. *The Review of Economics and Statistics*, pages 17–31, 1995.
- [15] P. Champsaur and J.P. Cotis. Rapport sur la situation des finances publiques, 2010. [http://www.elysee.fr/president/root/bank\\_objects/Rapport\\_Finances\\_publiques.pdf](http://www.elysee.fr/president/root/bank_objects/Rapport_Finances_publiques.pdf).
- [16] G.C. Chow and A.L. Lin. Best linear unbiased interpolation, distribution, and

- extrapolation of time series by related series. *The Review of Economics and Statistics*, 53(4):372–375, 1971.
- [17] European Commission. New and updated budgetary sensitivities for the EU budgetary surveillance. 2005.
  - [18] European Commission. Public finances in EMU. *European Economy*, 3, Sep. 2011.
  - [19] European Commission. Alert mechanism report. Feb. 2012.
  - [20] T. Davig. Periodically expanding discounted debt: a threat to fiscal policy sustainability? *Journal of Applied Econometrics*, 20(7):829–840, 2005.
  - [21] International Monetary Fund. Sustainability assessment. SM/02/166, 2002. Policy Development and Review Department.
  - [22] J.W. Galbraith, J. Dolado, and Banerjee A. Rejections of orthogonality in rational expectations models. Further Monte-Carlo results for an extended set of regressors. *Economics Letters*, 25:243–247, 1987.
  - [23] T. Guyon and S. Sorbe. Solde structurel et effort structurel : vers une décomposition par sous-secteur des administrations publiques, 2009. Document de travail de la DGTE N°2009/13.
  - [24] J.D. Hamilton and M.A. Flavin. On the limitations of government borrowing: A framework for empirical testing. *American Economic Review*, 76(4):808–819, Sep. 1986.
  - [25] G. Lamé, M. Lequien, and P.A. Pionnier. Interpretation and limits of sustainability tests in public finance. 2013. INSEE Working paper.
  - [26] M. Larch and A. Turrini. The cyclically-adjusted budget balance in EU fiscal policy making: A love at first sight turned into a mature relationship. *European Economy - Economic Papers*, 374, March 2009.
  - [27] N.G. Mankiw and M.D. Shapiro. Do we reject too often?: Small sample properties of tests of rational expectations models. *Economics Letters*, 20(2):139–145, 1986.
  - [28] E.G. Mendoza and J.D. Ostry. International evidence on fiscal solvency. Is fiscal policy “responsible”? *Journal of Monetary Economics*, 55:1081–1093, 2008.
  - [29] W.K. Newey and K.D. West. A simple, positive semi-definite, heteroskedasticity and autocorrelation consistent covariance matrix. *Econometrica*, 55:703–708, 1987.
  - [30] M. Pébereau. Des finances publiques au service de notre avenir. Rompre avec la facilité de la dette publique pour renforcer notre croissance et notre cohésion sociale, 2005. [http://www.minefi.gouv.fr/notes\\_bleues/nbb/nbb301/pebereau.pdf](http://www.minefi.gouv.fr/notes_bleues/nbb/nbb301/pebereau.pdf).
  - [31] C.E. Quintos. Sustainability of the deficit process with structural shifts. *Journal of Business & Economic Statistics*, pages 409–417, 1995.
  - [32] C.M. Reinhart and K.S. Rogoff. From financial crash to debt crisis. *American Economic Review*, 101(5):1676–1706, 2011. données utilisées: <http://www.aeaweb.org/issue.php?doi=10.1257/aer.101.5>.
  - [33] Y. Shin. A residual-based test of the null of cointegration against the alternative of non-cointegration. *Econometric Theory*, 10:91–115, 1994.
  - [34] C.A. Sims, J.H. Stock, and M.W. Watson. Inference in linear time series models with some unit roots. *Econometrica*, 58:113–144, 1990.
  - [35] J.H. Stock and M.W. Watson. Variable trends in economic time series. *The Journal of Economic Perspectives*, 2(3):147–174, 1988.
  - [36] J.H. Stock and M.W. Watson. A simple estimator of cointegrating vectors in

- higher order integrated systems. *Econometrica*, pages 783–820, 1993.
- [37] B. Trehan and C.E. Walsh. Common trends, the government’s budget constraint, and revenue smoothing. *Journal of Economic Dynamics and Control*, 12(2–3):425–444, 1988.
  - [38] B. Trehan and C.E. Walsh. Testing intertemporal budget constraints: theory and applications to US federal budget and current account deficits. *Journal of Money, Credit and Banking*, 23(2):206–223, 1991.
  - [39] D.W. Wilcox. The sustainability of government deficits: implications of the present-value borrowing constraint. *Journal of Money, Credit and Banking*, 21(3):291–306, 1989.
  - [40] C. Wyplosz. Debt sustainability assessment: the IMF approach and alternatives. 2007. HEI Working Paper.

G 9001	J. FAYOLLE et M. FLEURBAEY Accumulation, profitabilité et endettement des entreprises	G 9203	Macro-economic import functions with imperfect competition - An application to the E.C. Trade  I. STAPIC Les échanges internationaux de services de la France dans le cadre des négociations multilatérales du GATT Juin 1992 (1ère version) Novembre 1992 (version finale)	G 9311	J. BOURDIEU - B. COLIN-SEDILLOT Les décisions de financement des entreprises françaises : une évaluation empirique des théories de la structure optimale du capital	G 9412	analyse économique des politiques française et allemande
G 9002	H. ROUSSE Détection et effets de la multicolinéarité dans les modèles linéaires ordinaires - Un prolongement de la réflexion des BELSLEY, KUH et WELSCH			G 9312	L. BLOCH - B. CŒURÉ Q de Tobin marginal et transmission des chocs financiers	G 9413	J. BOURDIEU - B. CŒURÉ - B. COLIN-SEDILLOT Investissement, incertitude et irréversibilité Quelques développements récents de la théorie de l'investissement
G 9003	P. RALLE et J. TOUJAS-BERNATE Indexation des salaires : la rupture de 1983	G 9204	P. SEVESTRE L'économetric sur données individuelles-temporelles. Une note introductory	G 9313	Équipes Amadeus (INSEE), Banque de France, Métric (DP) Présentation des propriétés des principaux modèles macroéconomiques du Service Public	G 9414	B. DORMONT - M. PAUCHET L'évaluation de l'élasticité emploi-salaire dépend-elle des structures de qualification ?
G 9004	D. GUELLEC et P. RALLE Compétitivité, croissance et innovation de produit	G 9205	H. ERKEL-ROUSSE Le commerce extérieur et l'environnement international dans le modèle AMADEUS (réestimation 1992)	G 9314	B. CREPON - E. DUGUET Research & Development, competition and innovation	G 9501	I. KABLA Le Choix de breveter une invention
G 9005	P. RALLE et J. TOUJAS-BERNATE Les conséquences de la désindexation. Analyse dans une maquette prix-salaires	G 9206	N. GREENAN et D. GUELLEC Coordination within the firm and endogenous growth	G 9315	B. DORMONT Quelle est l'influence du coût du travail sur l'emploi ?	G 9502	J. BOURDIEU - B. CŒURÉ - B. SEDILLOT Irreversible Investment and Uncertainty: When is there a Value of Waiting?
G 9101	Équipe AMADEUS Le modèle AMADEUS - Première partie - Présentation générale	G 9207	A. MAGNIER et J. TOUJAS-BERNATE Technology and trade: empirical evidences for the major five industrialized countries	G 9316	D. BLANCHET - C. BROUSSE Deux études sur l'âge de la retraite	G 9503	L. BLOCH - B. CŒURÉ Imperfections du marché du crédit, investissement des entreprises et cycle économique
G 9102	J.L. BRILLET Le modèle AMADEUS - Deuxième partie - Propriétés variantielles	G 9208	B. CREPON, E. DUGUET, D. ENCAOUA et P. MOHNEN Cooperative, non cooperative R & D and optimal patent life	G 9317	D. BLANCHET Répartition du travail dans une population hétérogène : deux notes	G 9504	D. GOUX - E. MAURIN Les transformations de la demande de travail par qualification en France Une étude sur la période 1970-1993
G 9103	D. GUELLEC et P. RALLE Endogenous growth and product innovation	G 9209	B. CREPON et E. DUGUET Research and development, competition and innovation: an application of pseudo maximum likelihood methods to Poisson models with heterogeneity	G 9318	D. EYSSARTIER - N. PONTY AMADEUS - an annual macro-economic model for the medium and long term	G 9505	N. GREENAN Technologie, changement organisationnel, qualifications et emploi : une étude empirique sur l'industrie manufacturière
G 9104	H. ROUSSE Le modèle AMADEUS - Troisième partie - Le commerce extérieur et l'environnement international	G 9301	J. TOUJAS-BERNATE Commerce international et concurrence imparfaite : développements récents et implications pour la politique commerciale	G 9319	G. CETTE - Ph. CUNÉO - D. EYSSARTIER - J. GAUTIÉ Les effets sur l'emploi d'un abaissement du coût du travail des jeunes	G 9505 Bis	D. GOUX - E. MAURIN Persistance des hiérarchies sectorielles de salaires: un réexamen sur données françaises
G 9105	H. ROUSSE Effets de demande et d'offre dans les résultats du commerce extérieur manufacturé de la France au cours des deux dernières décennies	G 9302	Ch. CASES Durées de chômage et comportements d'offre de travail : une revue de la littérature	G 9401	D. BLANCHET Les structures par âge importent-elles ?	G 9506	D. GOUX - E. MAURIN Persistence of inter-industry wages differentials: a reexamination on matched worker-firm panel data
G 9106	B. CREPON Innovation, taille et concentration : causalités et dynamiques	G 9303	H. ERKEL-ROUSSE Union économique et monétaire : le débat économique	G 9402	J. GAUTIÉ Le chômage des jeunes en France : problème de formation ou phénomène de file d'attente ? Quelques éléments du débat	G 9507	S. JACOBZONE Les liens entre RMI et chômage, une mise en perspective NON PARU - article sorti dans <i>Économie et Prévision</i> n° 122 (1996) - pages 95 à 113
G 9107	B. AMABLE et D. GUELLEC Un panorama des théories de la croissance endogène	G 9304	N. GREENAN - D. GUELLEC / G. BROUSSAUDIER - L. MIOTTI Innovation organisationnelle, dynamisme technologique et performances des entreprises	G 9403	P. QUIRION Les déchets en France : éléments statistiques et économiques	G 9601	G. CETTE - S. MAHFOUZ Le partage primaire du revenu Constat descriptif sur longue période
G 9108	M. GLAUCHE et M. MOUTARDIER Une évaluation du coût direct de l'enfant de 1979 à 1989	G 9305	P. JAAILLARD Le traité de Maastricht : présentation juridique et historique	G 9404	D. LADIRAY - M. GRUN-REHOMME Lissage par moyennes mobiles - Le problème des extrémités de série	G 9602	Banque de France - CEPREMAP - Direction de la Prévision - Érasme - INSEE - OFCE Structures et propriétés de cinq modèles macroéconomiques français
G 9109	P. RALLE et alii France - Allemagne : performances économiques comparées	G 9306	J.L. BRILLET Micro-DMS : présentation et propriétés	G 9405	V. MAILLARD Théorie et pratique de la correction des effets de jours ouvrables	G 9603	Rapport d'activité de la DESE de l'année 1995
G 9110	J.L. BRILLET Micro-DMS <b>NON PARU</b>	G 9307	J.L. BRILLET Micro-DMS - variante : les tableaux	G 9406	F. ROSENWALD La décision d'investir	G 9604	J. BOURDIEU - A. DRAZNIEKS L'octroi de crédit aux PME : une analyse à partir d'informations bancaires
G 9111	A. MAGNIER Effets accélérateur et multiplicateur en France depuis 1970 : quelques résultats empiriques	G 9308	S. JACOBZONE Les grands réseaux publics français dans une perspective européenne	G 9407	S. JACOBZONE Les apports de l'économie industrielle pour définir la stratégie économique de l'hôpital public	G 9605	A. TOPIOL-BENSAÏD Les implantations japonaises en France
G 9112	B. CREPON et G. DUREAU Investissement en recherche-développement : analyse de causalités dans un modèle d'accélérateur généralisé	G 9309	L. BLOCH - B. CŒURE Profitabilité de l'investissement productif et transmission des chocs financiers	G 9408	L. BLOCH, J. BOURDIEU, B. COLIN-SEDILLOT, G. LONGUEVILLE Du défaut de paiement au dépôt de bilan : les banquiers face aux PME en difficulté	G 9606	P. GENIER - S. JACOBZONE Comportements de prévention, consommation d'alcool et tabagie : peut-on parler d'une gestion globale du capital santé ? Une modélisation microéconométrique empirique
G 9113	J.L. BRILLET, H. ERKEL-ROUSSE, J. TOUJAS-BERNATE "France-Allemagne Couplées" - Deux économies vues par une maquette macro-économétrique	G 9310	J. BOURDIEU - B. COLIN-SEDILLOT Les théories sur la structure optimale du capital : quelques points de repère	G 9409	D. EYSSARTIER, P. MAIRE Impacts macro-économiques de mesures d'aide au logement - quelques éléments d'évaluation	G 9607	C. DOZ - F. LENGLART Factor analysis and unobserved component models: an application to the study of French business surveys
G 9201	W.J. ADAMS, B. CREPON, D. ENCAOUA Choix technologiques et stratégies de dissuasion d'entrée			G 9410	F. ROSENWALD Suivi conjoncturel de l'investissement		N. GREENAN - D. GUELLEC La théorie coopérative de la firme
G 9202	J. OLIVEIRA-MARTINS, J. TOUJAS-BERNATE			G 9411	C. DEFEUILLEY - Ph. QUIRION Les déchets d'emballages ménagers : une		

G 9608	N. GREENAN - D. GUELLEC Technological innovation and employment reallocation	G 9714	F. LEQUILLER Does the French Consumer Price Index Overstate Inflation?	G 9807	Bilan des activités de la Direction des Études et Synthèses Économiques - 1997	Bis	Une estimation de l'élasticité de l'emploi peu qualifié à son coût
G 9609	Ph. COUR - F. RUPPRECHT L'intégration asymétrique au sein du continent américain : un essai de modélisation	G 9715	X. BONNET Peut-on mettre en évidence les rigidités à la baisse des salaires nominaux ? Une étude sur quelques grands pays de l'OCDE	G 9808	A. MOUROUGANE Can a Conservative Governor Conduct an Accommodative Monetary Policy?	G 9913	Division « Redistribution et Politiques Sociales » Le modèle de microsimulation dynamique DESTINIE
G 9610	S. DUCHENE - G. FORGEOT - A. JACQUOT Analyse des évolutions récentes de la productivité apparente du travail	G 9716	N. IUNG - F. RUPPRECHT Productivité de la recherche et rendements d'échelle dans le secteur pharmaceutique français	G 9809	X. BONNET - E. DUBOIS - L. FAUVET Asymétrie des inflations relatives et menus costs : tests sur l'inflation française	G 9914	E. DUGUET Macro-commandes SAS pour l'économétrie des panels et des variables qualitatives
G 9611	X. BONNET - S. MAHFOUZ The influence of different specifications of wages-prices spirals on the measure of the NAIRU: the case of France	G 9717	E. DUGUET - I. KABLA Appropriation strategy and the motivations to use the patent system in France - An econometric analysis at the firm level	G 9810	E. DUGUET - N. IUNG Sales and Advertising with Spillovers at the firm level: Estimation of a Dynamic Structural Model on Panel Data	G 9915	R. DUHAUTOIS Évolution des flux d'emplois en France entre 1990 et 1996 : une étude empirique à partir du fichier des bénéfices réels normaux (BRN)
G 9612	PH. COUR - E. DUBOIS, S. MAHFOUZ, J. PISANI-FERRY The cost of fiscal retrenchment revisited: how strong is the evidence?	G 9718	L.P. PELÉ - P. RALLE Âge de la retraite : les aspects incitatifs du régime général	G 9811	J.P. BERTHIER Congestion urbaine : un modèle de trafic de pointe à courbe débit-vitesse et demande élastique	G 9916	J.Y. FOURNIER Extraction du cycle des affaires : la méthode de Baxter et King
G 9613	A. JACQUOT Les flexions des taux d'activité sont-elles seulement conjoncturelles ?	G 9719	ZHANG Yingxiang - SONG Xueqing Lexique macroéconomique Français-Chinois, chinois-français	G 9812	C. PRIGENT La part des salaires dans la valeur ajoutée : une approche macroéconomique	G 9917	B. CRÉPON - R. DESPLATZ - J. MAIRESSE Estimating price cost margins, scale economies and workers' bargaining power at the firm level
G 9614	ZHANG Yingxiang - SONG Xueqing Lexique macroéconomique Français-Chinois	G 9720	M. HOUDEBINE - J.L. SCHNEIDER Mesurer l'influence de la fiscalité sur la localisation des entreprises	G 9813	A.Th. AERTS L'évolution de la part des salaires dans la valeur ajoutée en France reflète-t-elle les évolutions individuelles sur la période 1979-1994 ?	G 9918	Ch. GIANELLA - Ph. LAGARDE Productivity of hours in the aggregate production function: an evaluation on a panel of French firms from the manufacturing sector
G 9701	J.L. SCHNEIDER La taxe professionnelle : éléments de cadrage économique	G 9721	A. MOUROUGANE Crédibilité, indépendance et politique monétaire Une revue de la littérature	G 9814	B. SALANIÉ Guide pratique des séries non-stationnaires	G 9919	S. AUDRIC - P. GIVORD - C. PROST Évolution de l'emploi et des coûts par qualification entre 1982 et 1996
G 9702	J.L. SCHNEIDER Transition et stabilité politique d'un système redistributif	G 9722	P. AUGERAUD - L. BRION Les données comptables d'entreprises Le système intermédiaire d'entreprises Passage des données individuelles aux données sectorielles	G 9901	S. DUCHÈNE - A. JACQUOT Une croissance plus riche en emplois depuis le début de la décennie ? Une analyse en comparaison internationale	G 2000/01	R. MAHIEU Les déterminants des dépenses de santé : une approche macroéconomique
G 9703	D. GOUX - E. MAURIN Train or Pay: Does it Reduce Inequalities to Encourage Firms to Train their Workers?	G 9723	P. AUGERAUD - J.E. CHAPRON Using Business Accounts for Compiling National Accounts: the French Experience	G 9902	Ch. COLIN Modélisation des carrières dans Destinie	G 2000/02	C. ALLARD-PRIGENT - H. GUILMEAU - A. QUINET The real exchange rate as the relative price of nontrables in terms of tradables: theoretical investigation and empirical study on French data
G 9704	P. GENIER Deux contributions sur dépendance et équité	G 9724	P. AUGERAUD Les comptes d'entreprise par activités - Le passage aux comptes - De la comptabilité d'entreprise à la comptabilité nationale - A paraître	G 9903	Ch. COLIN Évolution de la dispersion des salaires : un essai de prospective par microsimulation	G 2000/03	J.-Y. FOURNIER L'approximation du filtre passe-bande proposée par Christiano and Fitzgerald
G 9705	E. DUGUET - N. IUNG R & D Investment, Patent Life and Patent Value An Econometric Analysis at the Firm Level	G 9801	H. MICHAUDON - C. PRIGENT Présentation du modèle AMADEUS	G 9904	B. CREPON - N. IUNG Innovation, emploi et performances	G 2000/04	Bilan des activités de la DESE - 1999
G 9706	M. HOUDEBINE - A. TOPIOL-BENSAÏD Les entreprises internationales en France : une analyse à partir de données individuelles	G 9802	J. ACCARDO Une étude de comptabilité générationnelle pour la France en 1996	G 9905	B. CREPON - Ch. GIANELLA Wages inequalities in France 1969-1992 An application of quantile regression techniques	G 2000/05	B. CREPON - F. ROSENWALD Investissement et contraintes de financement : le poids du cycle Une estimation sur données françaises
G 9707	M. HOUDEBINE Polarisation des activités et spécialisation des départements en France	G 9803	X. BONNET - S. DUCHÈNE Apports et limites de la modélisation « Real Business Cycles »	G 9906	C. BONNET - R. MAHIEU Microsimulation techniques applied to inter-generational transfers - Pensions in a dynamic framework: the case of France	G 2000/06	A. FLIPO Les comportements matrimoniaux de fait
G 9708	E. DUGUET - N. GREENAN Le biais technologique : une analyse sur données individuelles	G 9804	C. BARLET - C. DUGUET - D. ENCAOUA - J. PRADEL The Commercial Success of Innovations An econometric analysis at the firm level in French manufacturing	G 9907	F. ROSENWALD L'impact des contraintes financières dans la décision d'investissement	G 2000/07	R. MAHIEU - B. SÉDILLOT Microsimulations of the retirement decision: a supply side approach
G 9709	J.L. BRILLET Analyzing a small French ECM Model	G 9805	P. CAHUC - Ch. GIANELLA - D. GOUX - A. ZILBERBERG Equalizing Wage Differences and Bargaining Power - Evidence from a Panel of French Firms	G 9908	Bilan des activités de la DESE - 1998	G 2000/08	C. AUDENIS - C. PROST Déficit conjoncturel : une prise en compte des conjonctures passées
G 9710	J.L. BRILLET Formalizing the transition process: scenarios for capital accumulation	G 9806	J. ACCARDO - M. JLASSI La productivité globale des facteurs entre 1975 et 1996	G 9909	J.P. ZOYEM Contrat d'insertion et sortie du RMI Évaluation des effets d'une politique sociale	G 2000/09	R. MAHIEU - B. SÉDILLOT Équivalent patrimonial de la rente et souscription de retraite complémentaire
G 9711	G. FORGEOT - J. GAUTIÉ Insertion professionnelle des jeunes et processus de déclassement			G 9910	Ch. COLIN - FI. LEGROS - R. MAHIEU Bilans contributifs comparés des régimes de retraite du secteur privé et de la fonction publique	G 2000/10	R. DUHAUTOIS Ralentissement de l'investissement : petites ou grandes entreprises ? industrie ou tertiaire ?
G 9712	E. DUBOIS High Real Interest Rates: the Consequence of a Saving Investment Disequilibrium or of an insufficient Credibility of Monetary Authorities?			G 9911	G. LAROQUE - B. SALANIÉ Une décomposition du non-emploi en France	G 2000/11	G. LAROQUE - B. SALANIÉ Temps partiel féminin et incitations financières à l'emploi
G 9713	Bilan des activités de la Direction des Études et Synthèses Économiques - 1996			G 9912	B. SALANIÉ Une maquette analytique de long terme du marché du travail	G 2000/12	Ch. GIANELLA Local unemployment and wages

G2000/13	B. CREPON - Th. HECKEL - Informatisation en France : une évaluation à partir de données individuelles - Computerization in France: an evaluation based on individual company data	G2001/17	C. AUDENIS - P. BISCOURP - N. RIEDINGER Existe-t-il une asymétrie dans la transmission du prix du brut aux prix des carburants ?	G2002/15	P. CHONE - D. LE BLANC - I. ROBERT-BOBEE Offre de travail féminine et garde des jeunes enfants	G2004/05	N. RAGACHE La déclaration des enfants par les couples non mariés est-elle fiscalement optimale ?
G2001/01	F. LEQUILLER - La nouvelle économie et la mesure de la croissance du PIB - The new economy and the measurement of GDP growth	G2002/01	F. MAGNIEN - J.-L. TAVERNIER - D. THESMAR Les statistiques internationales de PIB par habitant en standard de pouvoir d'achat : une analyse des résultats	G2002/16	F. MAUREL - S. GREGOIR Les indices de compétitivité des pays : interprétation et limites	G2004/06	M. DUÉE L'impact du chômage des parents sur le devenir scolaire des enfants
G2001/02	S. AUDRIC La reprise de la croissance de l'emploi profite-t-elle aussi aux non-diplômés ?	G2002/02	Bilan des activités de la DESE - 2001	G2003/01	N. RIEDINGER - E. HAUVEY Le coût de dépollution atmosphérique pour les entreprises françaises : Une estimation à partir de données individuelles	G2004/07	P. AUBERT - E. CAROLI - M. ROGER New Technologies, Workplace Organisation and the Age Structure of the Workforce: Firm-Level Evidence
G2001/03	I. BRAUN-LEMAIRE Évolution et répartition du surplus de productivité	G2002/03	B. SÉDILLOT - E. WALRAET La cessation d'activité au sein des couples : y a-t-il interdépendance des choix ?	G2003/02	P. BISCOURP et F. KRAMARZ Création d'emplois, destruction d'emplois et internationalisation des entreprises industrielles françaises : une analyse sur la période 1986-1992	G2004/08	E. DUGUET - C. LELARGE Les brevets accroissent-ils les incitations privées à innover ? Un examen microéconométrique
G2001/04	A. BEAUDU - Th. HECKEL Le canal du crédit fonctionne-t-il en Europe ? Une étude de l'hétérogénéité des comportements d'investissement à partir de données de bilan agrégées	G2002/04	G. BRILHALT - Rétropolation des séries de FBCF et calcul du capital fixe en SEC-95 dans les comptes nationaux français - Retropolation of the investment series (GFCF) and estimation of fixed capital stocks on the ESA-95 basis for the French balance sheets	G2003/03	Bilan des activités de la DESE - 2002	G2004/09	S. RASPILLER - P. SILLARD Affiliating versus Subcontracting: the Case of Multinationals
G2001/05	C. AUDENIS - P. BISCOURP - N. FOURCADE - O. LOISEL Testing the augmented Solow growth model: An empirical reassessment using panel data	G2002/05	P. BISCOURP - B. CRÉPON - T. HECKEL - N. RIEDINGER How do firms respond to cheaper computers? Microeconometric evidence for France based on a production function approach	G2003/04	P.-O. BEFFY - J. DEROUYON - N. FOURCADE - S. GREGOIR - N. LAÏB - B. MONFORT Évolutions démographiques et croissance : une projection macro-économique à l'horizon 2020	G2004/10	J. BOISSINOT - C. L'ANGEVIN - B. MONFORT Public Debt Sustainability: Some Results on the French Case
G2001/06	R. MAHIEU - B. SÉDILLOT Départ à la retraite, irréversibilité et incertitude	G2002/06	C. AUDENIS - J. DEROUYON - N. FOURCADE L'impact des nouvelles technologies de l'information et de la communication sur l'économie française - un bouclage macro-économique	G2003/05	P. AUBERT La situation des salariés de plus de cinquante ans dans le secteur privé	G2004/11	S. ANANIAN - P. AUBERT Travailleurs âgés, nouvelles technologies et changements organisationnels : un réexamen à partir de l'enquête « REPONSE »
G2001/07	Bilan des activités de la DESE - 2000	G2002/07	J. BARDAJI - B. SÉDILLOT - E. WALRAET Évaluation de trois réformes du Régime Général d'assurance vieillesse à l'aide du modèle de microsimulation DESTINIE	G2003/06	P. AUBERT - B. CRÉPON Age, salaire et productivité La productivité des salariés décline-t-elle en fin de carrière ?	G2004/12	X. BONNET - H. PONCET Structures de revenus et propensions différentes à consommer - Vers une équation de consommation des ménages plus robuste en prévision pour la France
G2001/08	J. Ph. GAUDEMET Les dispositifs d'acquisition à titre facultatif d'annuités viagères de retraite	G2002/08	J.-P. BERTHIER Réflexions sur les différentes notions de volume dans les comptes nationaux : comptes aux prix d'une année fixe ou aux prix de l'année précédente, séries chainées	G2003/07	H. BARON - P.-O. BEFFY - N. FOURCADE - R. MAHIEU Le ralentissement de la productivité du travail au cours des années 1990	G2004/13	C. PICART Évaluer la rentabilité des sociétés non financières
G2001/09	B. CRÉPON - Ch. GIANELLA Fiscalité, coût d'usage du capital et demande de facteurs : une analyse sur données individuelles	G2002/09	F. HILD Les soldes d'opinion résument-ils au mieux les réponses des entreprises aux enquêtes de conjoncture ?	G2003/08	P.-O. BEFFY - B. MONFORT Patrimoine des ménages, dynamique d'allocation et comportement de consommation	G2004/14	J. BARDAJI - B. SÉDILLOT - E. WALRAET Les retraites du secteur public : projections à l'horizon 2040 à l'aide du modèle de microsimulation DESTINIE
G2001/10	B. CRÉPON - R. DESPLATZ Évaluation des effets des dispositifs d'allègements de charges sociales sur les bas salaires	G2002/10	I. ROBERT-BOBÉE Les comportements démographiques dans le modèle de microsimulation Destinie - Une comparaison des estimations issues des enquêtes Jeunes et Carrières 1997 et Histoire Familiale 1999	G2003/09	P. BISCOURP - N. FOURCADE Peut-on mettre en évidence l'existence de rigidités à la baisse des salaires à partir de données individuelles ? Le cas de la France à la fin des années 90	G2005/01	S. BUFFETEAU - P. GODEFROY Conditions de départ en retraite selon l'âge de fin d'études : analyse prospective pour les générations 1945 à 1974
G2001/11	J.-Y. FOURNIER Comparaison des salaires des secteurs public et privé	G2002/11	J.-P. ZOYEM La dynamique des bas revenus : une analyse des entrées-sorties de pauvreté	G2003/10	M. LECLAIR - P. PETIT Présence syndicale dans les firmes : quel impact sur les inégalités salariales entre les hommes et les femmes ?	G2005/02	C. AFSA - S. BUFFETEAU L'évolution de l'activité féminine en France : une approche par pseudo-panel
G2001/12	J.-P. BERTHIER - C. JAULENT R. CONVENEVOLE - S. PISANI Une méthodologie de comparaison entre consommations intermédiaires de source fiscale et de comptabilité nationale	G2002/12	F. HILD Prévisions d'inflation pour la France	G2003/11	P.-O. BEFFY - X. BONNET - M. DARRACQ-PARIES - B. MONFORT MZE: a small macro-model for the euro area	G2005/03	P. AUBERT - P. SILLARD Délocalisations et réductions d'effectifs dans l'industrie française
G2001/13	P. BISCOURP - Ch. GIANELLA Substitution and complementarity between capital, skilled and less skilled workers: an analysis at the firm level in the French manufacturing industry	G2002/13	M. LECLAIR Réduction du temps de travail et tensions sur les facteurs de production	G2004/01	P. AUBERT - M. LECLAIR La compétitivité exprimée dans les enquêtes trimestrielles sur la situation et les perspectives dans l'industrie	G2005/04	M. LECLAIR - S. ROUX Mesure et utilisation des emplois instables dans les entreprises
G2001/14	I. ROBERT-BOBÉE Modelling demographic behaviours in the French microsimulation model Destinie: An analysis of future change in completed fertility	G2002/14	E. WALRAET - A. VINCENT - Analyse de la redistribution intragénérationnelle dans le système de retraite des salariés du privé - Une approche par microsimulation - Intragenerational distributional analysis in the french private sector pension scheme - A microsimulation approach	G2004/02	M. DUÉE - C. REBILLARD La dépendance des personnes âgées : une projection à long terme	G2005/05	C. L'ANGEVIN - S. SERRAVALLE Performances à l'exportation de la France et de l'Allemagne - Une analyse par secteur et destination géographique
G2001/15	J.-P. ZOYEM Diagnostic sur la pauvreté et calendrier de revenus : le cas du "Panel européen des ménages"			G2004/03	S. RASPILLER - N. RIEDINGER Régulation environnementale et choix de localisation des groupes français	G2005/06	Bilan des activités de la Direction des Études et Synthèses Économiques - 2004
G2001/16	J.-Y. FOURNIER - P. GIVORD La réduction des taux d'activité aux âges extrêmes, une spécificité française ?			G2004/04	A. NABOULET - S. RASPILLER Les déterminants de la décision d'investir : une approche par les perceptions subjectives des firmes	G2005/07	S. RASPILLER La concurrence fiscale : principaux enseignements de l'analyse économique
						G2005/08	C. L'ANGEVIN - N. LAÏB Éducation et croissance en France et dans un panel de 21 pays de l'OCDE
						G2005/09	N. FERRARI Prévoir l'investissement des entreprises

G2005/10	P.-O. BEFFY - C. L'ANGEVIN Chômage et boucle prix-salaires : apport d'un modèle « qualifiés/peu qualifiés »	G2006/10	C. AFSA L'estimation d'un coût implicite de la pénibilité du travail chez les travailleurs âgés	G2008/02	P. BISOURP - X. BOUTIN - T. VERGÉ The Effects of Retail Regulations on Prices Evidence from the Loi Galland	G2009/07	S. QUANTIN - S. RASPILLER - S. SERRAVALLE Commerce intragroupe, fiscalité et prix de transferts : une analyse sur données françaises
G2005/11	B. HEITZ A two-states Markov-switching model of inflation in France and the USA: credible target VS inflation spiral	G2006/11	C. LELARGE Les entreprises (industrielles) françaises sont-elles à la frontière technologique ?	G2008/03	Y. BARBESOL - A. BRIANT Économies d'agglomération et productivité des entreprises : estimation sur données individuelles françaises	G2009/08	M. CLERC - V. MARCUS Élasticités-prix des consommations énergétiques des ménages
G2005/12	O. BIAU - H. ERKEL-ROUSSE - N. FERRARI Réponses individuelles aux enquêtes de conjoncture et prévision macroéconomiques : Exemple de la prévision de la production manufacturière	G2006/12	O. BIAU - N. FERRARI Théorie de l'opinion Faut-il pondérer les réponses individuelles ?	G2008/04	D. BLANCHET - F. LE GALLO Les projections démographiques : principaux mécanismes et retour sur l'expérience française	G2009/09	G. LALANNE - E. POULIQUEN - O. SIMON Prix du pétrole et croissance potentielle à long terme
G2005/13	P. AUBERT - D. BLANCHET - D. BLAU The labour market after age 50: some elements of a Franco-American comparison	G2006/13	A. KOUBI - S. ROUX Une réinterprétation de la relation entre productivité et inégalités salariales dans les entreprises	G2008/05	D. BLANCHET - F. TOUTLEMONDE Évolutions démographiques et déformation du cycle de vie active : quelles relations ?	G2009/10	D. BLANCHET - J. LE CACHEUX - V. MARCUS Adjusted net savings and other approaches to sustainability: some theoretical background
G2005/14	D. BLANCHET - T. DEBRAND - P. DOURGNON - P. POLLET L'enquête SHARE : présentation et premiers résultats de l'édition française	G2006/14	R. RATHÉLOT - P. SILLARD The impact of local taxes on plants location decision	G2008/06	M. BARLET - D. BLANCHET - L. CRUSSON Internationalisation et flux d'emplois : que dit une approche comptable ?	G2009/11	V. BELLAMY - G. CONSALES - M. FESSEAU - S. LE LAIDIER - É. RAYNAUD Une décomposition du compte des ménages de la comptabilité nationale par catégorie de ménage en 2003
G2005/15	M. DUÉE La modélisation des comportements démographiques dans le modèle de microsimulation DESTINIE	G2007/01	D. SRAER Allégements de cotisations patronales et dynamique salariale	G2008/07	C. LELARGE - D. SRAER - D. THESMAR Entrepreneurship and Credit Constraints - Evidence from a French Loan Guarantee Program	G2009/12	J. BARDAJI - F. TALLET Detecting Economic Regimes in France: a Qualitative Markov-Switching Indicator Using Mixed Frequency Data
G2005/16	H. RAQUI - S. ROUX Étude de simulation sur la participation versée aux salariés par les entreprises	G2007/02	V. ALBOUY - L. LEQUIEN Les rendements non monétaires de l'éducation : le cas de la santé	G2008/08	X. BOUTIN - L. JANIN Are Prices Really Affected by Mergers?	G2009/13	R. AEBERHARDT - D. FOUGÈRE - R. RATHÉLOT Discrimination à l'embauche : comment exploiter les procédures de testing ?
G2006/01	C. BONNET - S. BUFFETEAU - P. GODEFROY Disparités de retraite de droit direct entre hommes et femmes : quelques évolutions ?	G2007/03	D. BLANCHET - T. DEBRAND Aspiration à la retraite, santé et satisfaction au travail : une comparaison européenne	G2008/09	M. BARLET - A. BRIANT - L. CRUSSON Concentration géographique dans l'industrie manufacturière et dans les services en France : une approche par un indicateur en continu	G2009/14	Y. BARBESOL - P. GIVORD - S. QUANTIN Partage de la valeur ajoutée, approche par données microéconomiques
G2006/02	C. PICART Les gazelles en France	G2007/04	M. BARLET - L. CRUSSON Quel impact des variations du prix du pétrole sur la croissance française ?	G2008/10	M. BEFFY - É. COUDIN - R. RATHÉLOT Who is confronted to insecure labor market histories? Some evidence based on the French labor market transition	G2009/15	I. BUONO - G. LALANNE The Effect of the Uruguay round on the Intensive and Extensive Margins of Trade
G2006/03	P. AUBERT - B. CRÉPON - P. ZAMORA Le rendement apparent de la formation continue dans les entreprises : effets sur la productivité et les salaires	G2007/05	C. PICART Flux d'emploi et de main-d'œuvre en France : un réexamen	G2008/11	M. ROGER - E. WALRAET Social Security and Well-Being of the Elderly: the Case of France	G2010/01	C. MINODIER Avantages comparés des séries des premières valeurs publiées et des séries des valeurs révisées - Un exercice de prévision en temps réel de la croissance trimestrielle du PIB en France
G2006/04	J.-F. OUVRARD - R. RATHÉLOT Demographic change and unemployment: what do macroeconomic models predict?	G2007/06	V. ALBOUY - C. TAVAN Massification et démocratisation de l'enseignement supérieur en France	G2008/12	C. AFSA Analyser les composantes du bien-être et de son évolution Une approche empirique sur données individuelles	G2010/02	V. ALBOUY - L. DAVEZIES - T. DEBRAND Health Expenditure Models: a Comparison of Five Specifications Using Panel Data
G2006/05	D. BLANCHET - J.-F. OUVRARD Indicateurs d'engagements implicites des systèmes de retraite: chiffrements, propriétés analytiques et réactions à des chocs démographiques types	G2007/07	T. LE BARBANCHON The Changing response to oil price shocks in France: a DSGE type approach	G2008/13	M. BARLET - D. BLANCHET - T. LE BARBANCHON Microsimuler le marché du travail : un prototype	G2010/03	C. KLEIN - O. SIMON Le modèle MÉSANGE rééstimé en base 2000 Tome 1 – Version avec volumes à prix constants
G2006/06	G. BIAU - O. BIAU - L. ROUVIERE Nonparametric Forecasting of the Manufacturing Output Growth with Firm-level Survey Data	G2007/08	T. CHANEY - D. SRAER - D. THESMAR Collateral Value and Corporate Investment Evidence from the French Real Estate Market	G2009/01	P.-A. PIONNIER Le partage de la valeur ajoutée en France, 1949-2007	G2010/04	M.-É. CLERC - É. COUDIN L'IPC, miroir de l'évolution du coût de la vie en France ? Ce qu'apporte l'analyse des courbes d'Engel
G2006/07	C. AFSA - P. GIVORD Le rôle des conditions de travail dans les absences pour maladie	G2007/09	J. BOISSINOT Consumption over the Life Cycle: Facts for France	G2009/02	Laurent CLAVEL - Christelle MINODIER A Monthly Indicator of the French Business Climate	G2010/05	N. CECI-RENAUD - P.-A. CHEVALIER Les seuils de 10, 20 et 50 salariés : impact sur la taille des entreprises françaises
G2006/08	P. SILLARD - C. L'ANGEVIN - S. SERRAVALLE Performances comparées à l'exportation de la France et de ses principaux partenaires Une analyse structurelle sur 12 ans	G2007/10	C. AFSA Interpréter les variables de satisfaction : l'exemple de la durée du travail	G2009/03	H. ERKEL-ROUSSE - C. MINODIER Do Business Tendency Surveys in Industry and Services Help in Forecasting GDP Growth? A Real-Time Analysis on French Data	G2010/06	R. AEBERHARDT - J. POUGET National Origin Differences in Wages and Hierarchical Positions - Evidence on French Full-Time Male Workers from a matched Employer-Employee Dataset
G2006/09	X. BOUTIN - S. QUANTIN Une méthodologie d'évaluation comptable du coût du capital des entreprises françaises : 1984-2002	G2007/11	R. RATHÉLOT - P. SILLARD Zones Franches Urbaines : quels effets sur l'emploi salarié et les créations d'établissements ?	G2009/04	P. GIVORD - L. WILNER Les contrats temporaires : trappe ou marchepied vers l'emploi stable ?	G2010/07	S. BLASCO - P. GIVORD Les trajectoires professionnelles en début de vie active : quel impact des contrats temporaires ?
		G2007/12	V. ALBOUY - B. CRÉPON Aléa moral en santé : une évaluation dans le cadre du modèle causal de Rubin	G2009/05	G. LALANNE - P.-A. PIONNIER - O. SIMON Le partage des fruits de la croissance de 1950 à 2008 : une approche par les comptes de surplus	G2010/08	P. GIVORD Méthodes économétriques pour l'évaluation de politiques publiques
		G2008/01	C. PICART Les PME françaises : rentables mais peu dynamiques	G2009/06	L. DAVEZIES - X. D'HAUTFOEUILLE Faut-il pondérer ?... Ou l'éternelle question de l'économètre confronté à des données d'enquête		

G2010/09	P.-Y. CABANNES - V. LAPÈGUE - E. POULIQUEN - M. BEFFY - M. GAINI Quelle croissance de moyen terme après la crise ?	G2011/07	M. CLERC - M. GAINI - D. BLANCHET Recommendations of the Stiglitz-Sen-Fitoussi Report: A few illustrations	G2012/08	A. EIDELMAN - F. LANGUMIER - A. VICARD Prélèvements obligatoires reposant sur les ménages : des canaux redistributifs différents en 1990 et 2010
G2010/10	I. BUONO - G. LALANNE La réaction des entreprises françaises à la baisse des tarifs douaniers étrangers	G2011/08	M. BACHELET - M. BEFFY - D. BLANCHET Projeter l'impact des réformes des retraites sur l'activité des 55 ans et plus : une comparaison de trois modèles	G2012/09	O. BARGAIN - A. VICARD Le RMI et son successeur le RSA découragent-ils certains jeunes de travailler ? Une analyse sur les jeunes autour de 25 ans
G2010/11	R. RATHÉLOT - P. SILLARD L'apport des méthodes à noyaux pour mesurer la concentration géographique - Application à la concentration des immigrés en France de 1968 à 1999	G2011/09	C. LOUVOT-RUNAVOT L'évaluation de l'activité dissimulée des entreprises sur la base des contrôles fiscaux et son insertion dans les comptes nationaux	G2012/10	C. MARBOT - D. ROY Projections du coût de l'APA et des caractéristiques de ses bénéficiaires à l'horizon 2040 à l'aide du modèle Destinie
G2010/12	M. BARATON - M. BEFFY - D. FOUGÈRE Une évaluation de l'effet de la réforme de 2003 sur les départs en retraite - Le cas des enseignants du second degré public	G2011/10	A. SCHREIBER - A. VICARD La tertiarisation de l'économie française et le ralentissement de la productivité entre 1978 et 2008	G2012/11	A. MAUROUX Le crédit d'impôt dédié au développement durable : une évaluation économétrique
G2010/13	D. BLANCHET - S. BUFFETEAU - E. CRENNER S. LE MINEZ Le modèle de microsimulation Destinie 2 : principales caractéristiques et premiers résultats	G2011/11	M.-É. CLERC - O. MONSO - E. POULIQUEN Les inégalités entre générations depuis le baby-boom	G2012/12	V. COTTET - S. QUANTIN - V. RÉGNIER Coût du travail et allègements de charges : une estimation au niveau établissement de 1996 à 2008
G2010/14	D. BLANCHET - E. CRENNER Le bloc retraites du modèle Destinie 2 : guide de l'utilisateur	G2011/12	C. MARBOT et D. ROY Évaluation de la transformation de la réduction d'impôt en crédit d'impôt pour l'emploi de salariés à domicile en 2007	G2012/13	X. D'HAUTFOEUILLE, P. FEVRIER et L. WILNER Demand Estimation in the Presence of Revenue Management
G2010/15	M. BARLET - L. CRUSSON - S. DUPUCH - F. PUECH Des services échangés aux services échangeables : une application sur données françaises	G2011/13	P. GIVORD - R. RATHÉLOT - P. SILLARD Place-based tax exemptions and displacement effects: An evaluation of the Zones Franches Urbaines program	G2012/14	D. BLANCHET et S. LE MINEZ Joint macro/micro evaluations of accrued-to-date pension liabilities: an application to French reforms
G2010/16	M. BEFFY - T. KAMIONKA Public-private wage gaps: is civil-servant human capital sector-specific?	G2011/14	X. D'HAUTFOEUILLE - P. GIVORD - X. BOUTIN The Environmental Effect of Green Taxation: the Case of the French "Bonus/Malus"	G2013/01-F1301	T. DERROYON - A. MONTAUT et P-A PIONNIER Utilisation rétrospective de l'enquête Emploi à une fréquence mensuelle : apport d'une modélisation espace-état
G2010/17	P.-Y. CABANNES - H. ERKEL-ROUSSE - G. LALANNE - O. MONSO - E. POULIQUEN Le modèle Mésange réestimé en base 2000 Tome 2 - Version avec volumes à prix chaînés	G2011/15	M. BARLET - M. CLERC - M. GARNEO - V. LAPÈGUE - V. MARCUS La nouvelle version du modèle MZE, modèle macroéconométrique pour la zone euro	G2013/02-F1302	C. TRÉVIEN Habiter en HLM : quel avantage monétaire et quel impact sur les conditions de logement ?
G2010/18	R. AEBERHARDT - L. DAVEZIES Conditional Logit with one Binary Covariate: Link between the Static and Dynamic Cases	G2011/16	R. AEBERHARDT - I. BUONO - H. FADINGER Learning, Incomplete Contracts and Export Dynamics: theory and Evidence from French Firms	G2013/03	A. POISSONNIER Temporal disaggregation of stock variables - The Chow-Lin method extended to dynamic models
G2011/01	T. LE BARBANCHON - B. OURLIAC - O. SIMON Les marchés du travail français et américain face aux chocs conjoncturels des années 1986 à 2007 : une modélisation DSGE	G2011/17	C. KERDRAIN - V. LAPÈGUE Restrictive Fiscal Policies in Europe: What are the Likely Effects?	G2013/04	P. GIVORD - C. MARBOT Does the cost of child care affect female labor market participation? An evaluation of a French reform of childcare subsidies
G2011/02	C. MARBOT Une évaluation de la réduction d'impôt pour l'emploi de salariés à domicile	G2012/01	P. GIVORD - S. QUANTIN - C. TREVIEN A Long-Term Evaluation of the First Generation of the French Urban Enterprise Zones	G2013/05	G. LAME - M. LEQUIEN - P.-A. PIONNIER Interpretation and limits of sustainability tests in public finance
G2011/03	L. DAVEZIES Modèles à effets fixes, à effets aléatoires, modèles mixtes ou multi-niveaux : propriétés et mises en œuvre des modélisations de l'hétérogénéité dans le cas de données groupées	G2012/02	N. CECI-RENAUD - V. COTTET Politique salariale et performance des entreprises		
G2011/04	M. ROGER - M. WASMER Heterogeneity matters: labour productivity differentiated by age and skills	G2012/03	P. FÉVRIER - L. WILNER Do Consumers Correctly Expect Price Reductions? Testing Dynamic Behavior		
G2011/05	J.-C. BRICONGNE - J.-M. FOURNIER V. LAPÈGUE - O. MONSO De la crise financière à la crise économique L'impact des perturbations financières de 2007 et 2008 sur la croissance de sept pays industrialisés	G2012/04	M. GAINI - A. LEDUC - A. VICARD School as a shelter? School leaving-age and the business cycle in France		
G2011/06	P. CHARNOZ - É. COUDIN - M. GAINI Wage inequalities in France 1976-2004: a quantile regression analysis	G2012/05	M. GAINI - A. LEDUC - A. VICARD A scarred generation? French evidence on young people entering into a tough labour market		
		G2012/06	P. AUBERT - M. BACHELET Disparités de montant de pension et redistribution dans le système de retraite français		
		G2012/07	R. AEBERHARDT - P. GIVORD - C. MARBOT Spillover Effect of the Minimum Wage in France: An Unconditional Quantile Regression Approach		